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Measurement of Singly Cabibbo Suppressed Decays $\Lambda_{c}^{+}\rightarrow p\pi^{+}\pi^{-}$ and $\Lambda_{c}^{+}\rightarrow pK^{+}K^{-}$ M. Ablikim *et al.* (BESIII Collaboration)

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¹ Measurement of Singly Cabibbo-Suppressed Decays $\Lambda_c^+ \to p\pi^+\pi^-$ and $\Lambda_c^+ \to pK^+K^-$

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Using 567 pb⁻¹ of data collected with the BESIII detector at a center-of-mass energy of $\sqrt{s} = 4.599 \text{ GeV}$, near the $\Lambda_c^+ \bar{\Lambda}_c^-$ threshold, we study the singly Cabibbo-suppressed decays $\Lambda_c^+ \to p\pi^+\pi^-$ and $\Lambda_c^+ \to pK^+K^-$. By normalizing with respect to the Cabibbo-favored decay $\Lambda_c^+ \to p\pi^-\pi^+$, we obtain ratios of branching fractions: $\frac{\mathcal{B}(\Lambda_c^+ \to p\pi^+\pi^-)}{\mathcal{B}(\Lambda_c^+ \to pK^-\pi^+)} = (6.70 \pm 0.48 \pm 0.25)\%$, $\frac{\mathcal{B}(\Lambda_c^+ \to p\phi)}{\mathcal{B}(\Lambda_c^+ \to pK^-\pi^+)} = (1.81 \pm 0.33 \pm 0.13)\%$, and $\frac{\mathcal{B}(\Lambda_c^+ \to pK^+K_{non-\phi}^-)}{\mathcal{B}(\Lambda_c^+ \to pK^-\pi^+)} = (9.36 \pm 2.22 \pm 0.71) \times 10^{-3}$, where the uncertainties are statistical and systematic, respectively. The absolute branching fractions are also presented. Among these measurements, the decay $\Lambda_c^+ \to p\pi^+\pi^-$ is observed for the first time, and the precision of the branching fraction for $\Lambda_c^+ \to pK^+K_{non-\phi}^-$ and $\Lambda_c^+ \to p\phi$ is significantly improved.

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Hadronic decays of charmed baryons provide an ide-152 127 128 al laboratory to understand the interplay of the weak₁₅₃ and strong interaction in the charm region [1-9], which₁₅₄ 129 is complementary to charmed mesons. They also pro-vide essential input for studying the decays of *b*-flavored¹⁵⁵ 130 131 hadrons involving a Λ_c in the final state [10, 11]. In 132 contrast to the charmed meson decays, which are usu-133 ally dominated by factorizable amplitudes, decays of 134 charmed baryons receive sizable nonfactorizable contri-135 butions from W-exchange diagrams, which are subject to 136 color and helicity suppression. The study of nonfactoriz- $^{101}_{162}$ able contributions is critical to understand the dynamics $^{163}_{163}$ 137 138 of charmed baryons decays. 139

Since the first discovery of the ground state charmed 140 baryon Λ_c in 1979 [12, 13], progress with charmed ¹⁶⁵ baryons has been relatively slow, due to a scarcity of ¹⁶⁷ experimental data. Recently, based on an e^+e^- anni-¹⁶⁸ hilation data sample of 567 pb⁻¹ [14] at a center-of-¹⁶⁸ 141 142 143 144 mass (c.m.) energy of $\sqrt{s} = 4.599$ GeV, the BESIII¹⁶⁹ 145 Collaboration measured the absolute branching fractions¹⁷⁰ 146 (BF) of twelve Cabibbo-favored (CF) Λ_c^+ hadronic de-171 147 cays with a significantly improved precision [15]. For₁₇₂ 148 many other CF charmed baryon decay modes and most₁₇₃ 149 of the singly Cabibbo-suppressed (SCS) decays, however,174 150 no precision measurements are available; many of them175 151

even have not yet been measured [16]. As a consequence, we are not able to distinguish between the theoretical predictions among the different models [3–9].

The SCS decay $\Lambda_c^+ \to p\pi^+\pi^-$ proceeds via the external W-emission, internal W-emission and W-exchange processes, while the SCS decay $\Lambda_c^+ \to pK^+K^-$ proceeds via the internal W-emission and W-exchange diagrams only. Precisely measuring and comparing their BFs may help to reveal the Λ_c internal dynamics [1]. A measurement of the SCS mode $\Lambda_c^+ \to p\phi$ is of particular interest because it receives contributions only from the internal W-emission diagrams, which can reliably be obtained by a factorization approach [1]. An improved measurement of the $\Lambda_c^+ \to p\phi$ BF is thus essential to validate theoretical models and test the application of large- N_c factorization in the charmed baryon sector [17], where, N_c is the number of colors.

In this Letter, we describe a search for the SCS decays $\Lambda_c^+ \to p\pi^+\pi^-$ and present an improved measurement of the $\Lambda_c^+ \to pK^+K^-_{\text{non-}\phi}$ and $\Lambda_c^+ \to p\phi$ BFs. The BFs are measured relative to the CF mode $\Lambda_c^+ \to pK^-\pi^+$. Our analysis is based on the same data sample as that used in Ref. [15] collected by the BESIII detector. Details on the features and capabilities of the BESIII detector can

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¹⁷⁶ be found in Ref. [18]. Throughout this Letter, charge-233
¹⁷⁷ conjugate modes are implicitly included, unless otherwise234
¹⁷⁸ stated.

The GEANT4-based [19] Monte Carlo (MC) simula-236 179 tions of e^+e^- annihilations are used to understand the²³⁷ 180 backgrounds and to estimate detection efficiencies. The238 181 generator KKMC [20] is used to simulate the beam-239 182 energy spread and initial-state radiation (ISR) of the240 183 e^+e^- collisions. The inclusive MC sample includes $\Lambda_c^+\bar\Lambda_c^-{}^{_{241}}$ 184 events, charmed meson $D_{(s)}^{(*)}$ pair production, ISR re-²⁴² 185 turns to lower-mass ψ states, and continuum processes 186 $e^+e^- \to q\bar{q} \ (q=u,d,s)$. Decay modes as specified in the 187 PDG [16] are modeled with EVTGEN [21, 22]. Signal 188 MC samples of $e^+e^- \to \Lambda_c^+ \bar{\Lambda}_c^-$ are produced in which the 189 Λ_c^+ decays to the interested final state $(pK^-\pi^+, p\pi^+\pi^-)$ 190 or pK^+K^-) together with the $\bar{\Lambda}_c^-$ decaying generically 191 to all possible final states. 192

Charged tracks are reconstructed from hits in the MDC 193 and are required to have polar angles within $|\cos\theta| < |\cos\theta|$ 194 0.93. The points of closest approach of the charged tracks 195 to the interaction point (IP) are required to be within 1 196 cm in the plane perpendicular to the beam (V_r) and ± 10 197 cm along the beam (V_z) . Information from the TOF sys-198 tem and dE/dx in the MDC are combined to form PID 199 confidence levels (C.L.) for the π , K and p hypotheses. 200 Each track is assigned to the particle type with the high-201 est PID C.L.. To avoid backgrounds from beam interac-202 tions with residual gas or detector materials (beam pipe 203 and MDC inner wall), a further requirement $V_r < 0.2$ cm 204 is imposed for proton. 205

 Λ_c^+ candidates are reconstructed by considering all 206 combinations of charged tracks in the final states of in-207 terest $pK^{-}\pi^{+}$, $p\pi^{+}\pi^{-}$ and $pK^{+}K^{-}$. Two variables, 208 the energy difference $\Delta E = E - E_{\text{beam}}$ and the beam-constrained mass $M_{\text{BC}} = \sqrt{E_{\text{beam}}^2/c^4 - p^2/c^2}$, are used²⁴³ to identify the Λ_c^+ candidates. Here, E_{beam} is the beam²⁴⁵ 209 210 211 energy, and E(p) is the reconstructed energy (momen-²⁴⁵ 212 tum) of the Λ_c^+ candidate in the e^+e^- c.m. system. A 213 Λ_c^+ candidate is accepted with $M_{\rm BC} > 2.25 {\rm GeV}/c^2$ and²⁴⁷ 214 $|\Delta E| < 20$ MeV (corresponding to 3 time of resolution).²⁴⁸ 215 For a given signal mode, we accept only one candidate per 216 Λ_c charge per event. If multiple candidates are found, the $^{\rm 250}$ 217 one with the smallest $|\Delta E|$ is selected. The ΔE sideband²⁵¹ 218 region, $40 < |\Delta E| < 60$ MeV, is defined to investigate²⁵² 219 potential backgrounds. 220

For the $\Lambda_c^+ \to p\pi^+\pi^-$ decay, we reject K_S^0 and Λ candidates by requiring $|M_{\pi^+\pi^-} - M_{K_S^0}^{PDG}| > 15 \text{ MeV}/c_{256}^{255}$ and $|M_{p\pi^-} - M_{\Lambda}^{PDG}| > 6 \text{ MeV}/c^2$, corresponding to 3_{257} times of the resolution, where $M_{K_S^0}^{PDG}$ (M_{Λ}^{PDG}) is the K_S^0 (Λ) mass quoted from the PDG [16] and $M_{\pi^+\pi^-}^{259}$ ($M_{p\pi^-}$) is the $\pi^+\pi^-$ ($p\pi^-$) invariant mass. These re-²⁶⁰ quirements suppress the peaking backgrounds of the CF²⁶¹ decays $\Lambda_c^+ \to \Lambda\pi^+$ and $\Lambda_c^+ \to pK_S^0$, which have the same²⁶² final state as the signal.

With the above selection criteria, the $M_{\rm BC}$ distribu-264 tions are depicted in Fig. 1 for the decays $\Lambda_c^+ \to p K^- \pi^+_{265}$ and $\Lambda_c^+ \to p \pi^+ \pi^-$ and in Fig. 2 (a) for the decay266 $\Lambda^+_c \to pK^+K^-$. Prominent Λ^+_c signals are observed. The inclusive MC samples are used to study potential backgrounds. For the decays $\Lambda^+_c \to pK^-\pi^+$ and $\Lambda^+_c \to pK^+K^-$, no peaking background is evidenced in the $M_{\rm BC}$ distributions. While for the decay $\Lambda^+_c \to p\pi^+\pi^-$, the peaking backgrounds of 28.2 ± 1.6 events from the decays $\Lambda^+_c \to \Lambda\pi^+$ and $\Lambda^+_c \to pK^0_S$ are expected, where the uncertainty comes from the measured BFs in Ref. [15]. The cross feed between the decay modes is negligible by the MC studies.



FIG. 1. (color online). Distributions of $M_{\rm BC}$ for the decays (a) $\Lambda_c^+ \to p K^- \pi^+$ and (b) $\Lambda_c^+ \to p \pi^+ \pi^-$. Points with error bar are data, the blue solid lines show the total fits, the blue long dashed lines are the combinatorial background shapes, and the red long dashed histograms are data from the ΔE sideband region for comparison. In (b), the green shaded histogram is the peaking background from the CF decays $\Lambda_c^+ \to p K_S^0$ and $\Lambda_c^+ \to \Lambda \pi^+$. The insert plot in (b) shows the $\pi^+\pi^-$ invariant mass distribution with additional requirement $|\Delta E| < 8$ MeV and 2.2836 $< M_{BC} < 2.2894$ GeV/ c^2 , where the dots with error bar are for the data, the blue solid histogram shows the fit curve from PWA, and the green shaded histogram shows background estimated from the M_{BC} sideband region.

To obtain the signal yields of the decays $\Lambda_c^+ \to p K^- \pi^+$ and $\Lambda_c^+ \to p \pi^+ \pi^-$, a maximum likelihood fit is performed to the corresponding $M_{\rm BC}$ distributions. The signal shape is modeled with the MC simulated shape convoluted with a Gaussian function representing the resolution difference and potential mass shift between the data and MC simulation. The combinatorial background is modeled by an ARGUS function [23]. In the decay $\Lambda_c^+ \to p \pi^+ \pi^-$, the peaking background is included in the fit, and is modeled with the MC simulated shape convoluted with the same Gaussian function for the signal, while the magnitude is fixed to the MC prediction. The fit curves are shown in Fig. 1. The $M_{\rm BC}$ distribution for events in the ΔE sideband region is also shown in Fig. 1(b) and a good agreement with the fitted background shape is indicated. The signal yields are summarized in Table I.

For the decay $\Lambda_c^+ \to pK^+K^-$, a prominent ϕ signal is observed in the $M_{K^+K^-}$ distribution, as shown in Fig. 2 (b). To determine the signal yields via ϕ (N_{sig}^{ϕ}) and non- ϕ $(N_{\text{sig}}^{\text{non-}\phi})$ processes, and to better model the background, we perform a two-dimensional unbinned extended maximum likelihood fit to the M_{BC} versus $M_{K^+K^-}$ distributions for events in the ΔE signal region and sideband re-



FIG. 2. (color online). Distributions of $M_{\rm BC}$ (left) and₂₉₅ $M_{K^+K^-}$ (right) for data in the ΔE signal region (upper) and₂₉₆ sideband region (bottom) for the decay $\Lambda_c^+ \to pK^+K^-$. The₂₉₇ blue solid curves are for the total fit results, the red dashdotted curves show the $\Lambda_c^+ \to p\phi \to pK^+K^-$ signal, the green²⁹⁹ dotted curves show the $\Lambda_c^+ \to pK^+K^-_{\text{non-}\phi}$ signal, the blue²⁹⁹ long-dashed curves are the background with ϕ production, and the magenta dashed curves are the non- ϕ background.

gion simultaneously. In the M_{BC} distribution, the shapes 267 of Λ_c signal (via ϕ or non- ϕ process) and background, de-268 noted as $S_{M_{\rm BC}}$ and $B_{M_{\rm BC}}$, are modeled similarly to those in the decay $\Lambda_c^+ \to p\pi^+\pi^-$. In the $M_{K^+K^-}$ distribution, the ϕ shape for the Λ_c process $(\Lambda_c^+ \to p\phi \to pK^+K^-)$, 269 270 271 $\mathbf{S}^{\phi}_{M_{KK}},$ is modeled with a relativistic Breit-Wigner func-272 tion convoluted with a Gaussian function representing 273 the detector resolution, while that for the Λ_c decay with-out ϕ ($\Lambda_c^+ \to pK^+K^-$), $S_{M_{KK}}^{\text{non-}\phi}$, is represented by the₃₀₁ 274 275 MC shape with a uniform distribution in K^+K^- phase₃₀₂ 276 space. The shape for the non- Λ_c background including $\phi_{\scriptscriptstyle 303}$ 277 state, $B^{\phi}_{M_{KK}}$, has the same parameters as $S^{\phi}_{M_{KK}}$, while₃₀₄ 278 that for the background without ϕ , $B_{M_{KK}}^{\text{non-}\phi}$, is described³⁰⁵ by a 3rd-order polynomial function. Detailed MC studies³⁰⁶ 279 280 indicate the non- Λ_c background (both with and without³⁰⁷ 281 ϕ included) have the same shapes and yields in both ΔE^{308} 282 signal and sideband regions, where the yields are denoted $^{\scriptscriptstyle 309}$ 283 as N_{bkg}^{ϕ} and $N_{bkg}^{non-\phi}$, respectively. The Likelihoods for³¹⁰ the events in ΔE signal and sideband regions are given³¹¹ 284 285 312 in equation (1) and (2), respectively. 286 313

$$\mathcal{L}_{\text{sig}} = \frac{e^{-(N_{\text{sig}}^{\phi} + N_{\text{sig}}^{\text{non-}\phi} + N_{\text{bkg}}^{\phi} + N_{\text{bkg}}^{\text{non-}\phi})}}{N_{\text{sig}}!}$$

$$= \frac{N_{\text{sig}}^{N_{\text{sig}}} N_{\text{sig}}!}{N_{\text{sig}}!}$$

$$= \frac{N_{\text{sig}}^{N_{\text{sig}}} N_{\text{sig}}!}{N_{\text{sig}}!}$$

$$= \frac{N_{\text{sig}}^{N_{\text{sig}}} N_{\text{BC}}(M_{\text{BC}}^{i}) \times S_{M_{KK}}^{\phi}(M_{K^{+}K^{-}}^{i})}{N_{\text{sig}}!}$$

$$= \frac{N_{\text{sig}}^{non-\phi} S_{M_{\text{BC}}}(M_{\text{BC}}^{i}) \times S_{M_{KK}}^{non-\phi}(M_{K^{+}K^{-}}^{i})}{N_{\text{bkg}}!}$$

$$= \frac{N_{\text{bkg}}^{\phi} B_{M_{\text{BC}}}(M_{\text{BC}}^{i}) \times B_{M_{KK}}^{\phi}(M_{K^{+}K^{-}}^{i})}{N_{\text{bkg}}!}$$

$$= \frac{N_{\text{bkg}}^{\phi} B_{M_{\text{BC}}}(M_{\text{BC}}^{i}) \times B_{M_{KK}}^{non-\phi}(M_{K^{+}K^{-}}^{i})}{N_{\text{bkg}}!}$$

$$\mathcal{L}_{\text{side}} = \frac{e^{-(N_{\text{bkg}}^{\phi} + N_{\text{bkg}}^{\text{non-}\phi})}}{N_{\text{side}}}$$

$$\times \prod_{i=1}^{N_{\text{side}}} [N_{\text{bkg}}^{\phi} B_{M_{\text{BC}}}(M_{\text{BC}}^{i}) \times B_{M_{KK}}^{\phi}(M_{K^{+}K^{-}}^{i})$$

$$+ N_{\text{bkg}}^{\text{non-}\phi} B_{M_{\text{BC}}}(M_{\text{BC}}^{i}) \times B_{M_{KK}}^{\text{non-}\phi}(M_{K^{+}K^{-}}^{i})], (2)$$

where the parameter $N_{\rm sig}$ ($N_{\rm side}$) is the total number of selected candidates in the ΔE signal (sideband) region, and $M_{\rm BC}^i$ and $M_{K^+K^-}^i$ are the values of $M_{\rm BC}$ and $M_{K^+K^-}$ for the *i*-th event. We use the product of PDFs, since the $M_{\rm BC}$ and $M_{K^+K^-}$ are verified to be uncorrelated for each component by MC simulations.

The signal yields are extracted by minimizing the negative log-likelihood $-\ln \mathcal{L} = (-\ln \mathcal{L}_{sig}) + (-\ln \mathcal{L}_{side})$. The fit curves are shown in Fig. 2 and the yields are listed in Table I. The significance is estimated by comparing the likelihood values with and without the signal components included, incorporating with the change of the number of free parameters, listed in Table I.

TABLE I. Summary of signal yields in data (N_{signal}), detection efficiencies (ε), and the significances. The errors are statistical only.

Decay modes	$N_{\rm signal}$	$\varepsilon(\%)$	significance
$\Lambda_c^+ \to p K^- \pi^+$	5940 ± 85	48.0 ± 0.1	-
$\Lambda_c^+ \to p \pi^+ \pi^-$	495 ± 35	59.7 ± 0.1	16.2σ
$\Lambda_c^+ \to p K^+ K^- (\text{via } \phi)$	44 ± 8	40.2 ± 0.1	9.6σ
$\Lambda_c^+ \to p K^+ K^- (\text{non-}\phi)$	38 ± 9	32.7 ± 0.1	5.4σ

In the decays $\Lambda_c^+ \to p K^- \pi^+$ and $\Lambda_c^+ \to p \pi^+ \pi^-$, the detection efficiencies are estimated with data-driven MC samples generated according to the results of a simple partial wave analysis (PWA) by the covariant helicity coupling amplitude [24, 25] for the quasi-two body decays. In the decay $\Lambda_c^+ \to p \pi^+ \pi^-$, prominent structures arising from $\rho^0(770)$ and $f_0(980)$ resonances are observed in the $M_{\pi^+\pi^-}$ distribution as shown in the insert plot of Fig. 1(b), and are included in PWA. Due to the limited statistics and relatively high background, the PWA does not allow for a reliable extraction of BFs for intermediate states; it however does describe the kinematics well and it is reasonable for the estimation of the detection efficiency. The corresponding uncertainty is taken into account as a systematic error. For the decays $\Lambda_c^+ \to p K^+ K^-$ via ϕ or non- ϕ , the detection efficiencies are estimated with phase space MC samples, where the angular distribution of the decay $\phi \to K^+ K^-$ is considered.

We measure the relative BFs of the SCS decays with respect to that of the CF decay $\Lambda_c^+ \rightarrow pK^-\pi^+$, and the absolute BFs by incorporating $\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+) =$ $(5.84 \pm 0.27 \pm 0.23)\%$ from the most recent BESIII measurement [15]. Several sources of systematic uncertainty, including tracking and PID efficiencies, the total number of $\Lambda_c^+\bar{\Lambda}_c^-$ pairs in data, cancel when calculating the ratio of BFs, due to the similar kinematics between the₃₆₈

326 SCS and CF decays. When calculating these uncertain-369

327 ties, cancellation has been taken into account whenever 370

328 pos

possible.

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TABLE II. The systematic uncertainties (in %) in the relative $^{374}_{374}$ BF measurements. The uncertainty of the reference BF $\mathcal{B}_{ref._{375}}$ applies only to the absolute BF measurements.

Sources	$\Lambda_c^+ \to p \pi^+ \pi^-$	$\Lambda_c^+ \to p\phi$	$\Lambda_c^+ \to p K^+ K_{\text{non-}\phi}^-$
Tracking	1.1	2.6	1.6
PID	1.3	1.5	1.9
V_r requirement	0.6	2.5	2.5
K_S^0/Λ vetoes	0.7	_	_
ΔE requirement	0.5	0.7	0.9
Fit	2.7	5.8	6.6
Cited BR	_	1.0	_
MC model	1.4	1.0	1.1
MC statistics	0.3	0.4	0.4
Total	3.7	7.2	7.6
$\mathcal{B}_{\mathrm{ref.}}$	6.1	6.1	6.1

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The uncertainties associated with tracking and PID³⁸⁹ 331 efficiencies for π , K and proton are studied as a func-³⁹⁰ 332 tion of (transverse) momentum with samples of $e^+e^- \rightarrow^{_{391}}$ 333 $\pi^+\pi^-\pi^+\pi^-$, $K^+K^-\pi^+\pi^-$ and $p\bar{p}\pi^+\pi^-$ from data taken³⁹² 334 at $\sqrt{s} > 4.0$ GeV. To extract tracking efficiency for par-³⁹³ 335 ticle *i* ($i = \pi$, K, or ptoton), we select the corresponding³⁹⁴ 336 samples by missing particle i with high purity, the ratio³⁹⁵ 337 to find the track i around the missing direction is the³⁹⁶ 338 tracking efficiency. Similarly, we select the control sam-397 330 ple without PID requirement for particle i, and then the³⁹⁸ 340 PID requirement is further implemented. The PID effi-³⁹⁹ 341 ciency is the ratio between the number of candidate with⁴⁰⁰ 342 and without PID requirement. The differences on the401 343 efficiency between the data and MC simulation weight-402 344 ed by the (transverse) momentum according to data are₄₀₃ 345 assigned as uncertainties. 346

The uncertainties due to the V_r requirements and₄₀₅ 347 K_S^0/Λ vetoes (in $\Lambda_c^+ \to p\pi^+\pi^-$ only) are investigated₄₀₆ 348 by repeating the analysis with alternative requirements₄₀₇ $(V_r < 0.25 \text{ cm}, |M_{\pi^+\pi^-} - M_{K_S^0}^{\text{PDG}}| > 20 \text{ MeV}/c^2 \text{ and}_{408}$ 349 350 $|M_{p\pi^-} - M_{\Lambda}^{\text{PDG}}| > 8 \text{ MeV}/c^2$, respectively). The result-409 351 ing differences in the BF are taken as the uncertainties.⁴¹⁰ 352 Uncertainties related to the ΔE resolution are estimat-411 353 ed by widening the ΔE windows from 3σ to 4σ of the⁴¹² 354 resolution. 413 355

For the decays $\Lambda_c^+ \to p K^- \pi^+$ and $\Lambda_c^+ \to p \pi^+ \pi^-$, the⁴¹⁴ 356 signal yields are determined from fits to the $M_{\rm BC}$ dis-415 357 tributions. Alternative fits are carried out by varying⁴¹⁶ 358 the fit range, signal shape, background shape and the417 359 expected number of peaking background. The resultant⁴¹⁸ 360 changes in the BFs are taken as uncertainties. In the₄₁₉ 361 decay $\Lambda_c^+ \to p K^+ K^-$, the uncertainties associated with₄₂₀ 362 the fit are studied by varying the fit ranges, signal and₄₂₁ 363 background shapes for both the $M_{\rm BC}$ and $M_{K^+K^-}$ dis-422 364 tributions and ΔE sideband region. 365 423

The following four aspects are considered for the MC_{424} simulation model uncertainty. *a*) The uncertainties relat-425

ed to the beam energy spread are investigated by changing its value in simulation by ± 0.4 MeV, where the nominal values is 1.5 MeV determined by data. The larger change in the measurement is taken as systematic uncertainty. b) The uncertainties associated with the input line shape of $e^+e^- \to \Lambda_c^+ \bar{\Lambda}_c^-$ cross section is estimated by replacing the line shape directly from BESIII data with that from Ref. [26]. c) The Λ_c^+ polar angle distribution in e^+e^- rest frame is parameterized with $1 + \alpha \cos^2 \theta$, where the α value is extracted from data. The uncertainties due to the Λ_c^+ polar angle distribution is estimated by changing α value by one standard deviation. d) The decays $\Lambda_c^+ \to p K^- \pi^+$ and $\Lambda_c^+ \to p \pi^+ \pi^-$ are modeled by a data-driven method according to PWA results. The corresponding uncertainties are estimated by changing the intermediate states included, changing the parameters of the intermediate states by one standard deviation quoted in the PDG [16], and varying the background treatment in the PWA and the output parameters for the coupling. Assuming all of the above PWA uncertainties are independent, the uncertainty related to MC modelling is the quadratic sum of all individual values. For the non- ϕ decay $\Lambda_c^+ \to p K^+ K^-$, phase space MC samples with Swave for K^+K^- pair is used to estimate the detection efficiency. An alternative MC sample with *P*-wave between K^+K^- pair is also used, and the resultant difference in efficiency is taken as the uncertainty. The uncertainties due to limited MC statistics in both the measured and reference modes are taken into account.

Assuming all uncertainties, summarized in Table II, are independent, the total uncertainties in the relative BF measurements are obtained by adding the individual uncertainties in quadrature. For the absolute BF measurements, the uncertainty due to the reference BF $\mathcal{B}_{ref.}(\Lambda_c^+ \to pK^-\pi^+)$, listed in Table II too, is included.

In summary, based on 567 pb⁻¹ of e^+e^- annihilation data collected at $\sqrt{s} = 4.599$ GeV with the BESIII detector, we present the first observation of the SCS decays $\Lambda_c^+ \to p\pi^+\pi^-$, and improved (or comparable) measurements of the $\Lambda_c^+ \to p\phi$ and $\Lambda_c^+ \to pK^+K_{\text{non-}\phi}^-$ BFs comparing to PDG values [16]. The relative BFs with respect to the CF decay $\Lambda_c^+ \to pK^-\pi^+$ are measured. Taking $\mathcal{B}(\Lambda_c^+ \to pK^-\pi^+) = (5.84 \pm 0.27 \pm 0.23)\%$ from Ref. [15], we also obtain absolute BFs for the SCS decays. All the results are summarized in Table III. The results provide important data to understand the dynamics of Λ_c^+ decays. They especially help to distinguish predictions from different theoretical models and understand contributions from factorizable effects [1].

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Decay modes	$\mathcal{B}_{\mathrm{mode}}/\mathcal{B}_{\mathrm{ref.}}$ (This work)	$\mathcal{B}_{\rm mode}/\mathcal{B}_{\rm ref.}$ (PDG average)
$\Lambda_c^+ \to p \pi^+ \pi^-$	$(6.70 \pm 0.48 \pm 0.25) \times 10^{-2}$	$(6.9 \pm 3.6) \times 10^{-2}$
$\Lambda_c^+ \to p\phi$	$(1.81 \pm 0.33 \pm 0.13) \times 10^{-2}$	$(1.64 \pm 0.32) \times 10^{-2}$
$\Lambda_c^+ \to p K^+ K^- \text{ (non-}\phi\text{)}$	$(9.36 \pm 2.22 \pm 0.71) \times 10^{-3}$	$(7 \pm 2 \pm 2) \times 10^{-3}$
_	$\mathcal{B}_{\text{mode}}$ (This work)	$\mathcal{B}_{\text{mode}}$ (PDG average)
$\Lambda_c^+ \to p \pi^+ \pi^-$	$(3.91 \pm 0.28 \pm 0.15 \pm 0.24) \times 10^{-3}$	$(3.5 \pm 2.0) \times 10^{-3}$
$\Lambda_c^+ \to p\phi$	$(1.06 \pm 0.19 \pm 0.08 \pm 0.06) \times 10^{-3}$	$(8.2 \pm 2.7) \times 10^{-4}$
$\Lambda_c^+ \to p K^+ K^- \text{ (non-}\phi\text{)}$	$(5.47 \pm 1.30 \pm 0.41 \pm 0.33) \times 10^{-4}$	$(3.5 \pm 1.7) \times 10^{-4}$

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TABLE III. Summary of relative and absolute BFs, and comparing with the results from PDG [16]. Uncertainties are statistical, experimental systematic, and reference mode uncertainty, respectively.

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