## Study of the decays $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda+$ c.c. and $\boldsymbol{\psi}(\mathbf{3 6 8 6}) \rightarrow \bar{p} K^{*+} \Lambda+$ c.c.

M. Ablikim, ${ }^{1}$ M. N. Achasov, ${ }^{10, \mathrm{~d}}$ P. Adlarson, ${ }^{59}$ S. Ahmed, ${ }^{15}$ M. Albrecht, ${ }^{4}$ M. Alekseev, ${ }^{58 \mathrm{a}, 58 \mathrm{c}}$ A. Amoroso, ${ }^{58 \mathrm{a}, 58 \mathrm{c}}$ F. F. An ${ }^{1}$ Q. An, ${ }^{55,43}$ Y. Bai, ${ }^{42}$ O. Bakina, ${ }^{27}$ R. Baldini Ferroli, ${ }^{23 a}$ Y. Ban, ${ }^{35}$ K. Begzsuren, ${ }^{25}$ J. V. Bennett, ${ }^{5}$ N. Berger, ${ }^{26}$ M. Bertani, ${ }^{23 a}$ D. Bettoni, ${ }^{24 \mathrm{a}}$ F. Bianchi, ${ }^{58 \mathrm{a}, 58 \mathrm{c}}$ J. Biernat, ${ }^{59}$ J. Bloms, ${ }^{52}$ I. Boyko, ${ }^{27}$ R. A. Briere,${ }^{5}$ H. Cai, ${ }^{60}$ X. Cai, ${ }^{1,43}$ A. Calcaterra, ${ }^{23 \mathrm{a}}$ G. F. Cao, ${ }^{1,47}$ N. Cao, ${ }^{1,47}$ S. A. Cetin, ${ }^{46 \mathrm{~b}}$ J. Chai, ${ }^{58 \mathrm{c}}$ J. F. Chang, ${ }^{1,43}$ W. L. Chang, ${ }^{1,47}$ G. Chelkov, ${ }^{27, b, c}$ D. Y. Chen, ${ }^{6}$ G. Chen, ${ }^{1}$
H. S. Chen, ${ }^{1,47}$ J. C. Chen, ${ }^{1}$ M. L. Chen, ${ }^{1,43}$ S. J. Chen, ${ }^{33}$ Y. B. Chen, ${ }^{1,43}$ W. Cheng, ${ }^{58 c}$ G. Cibinetto, ${ }^{24 a}$ F. Cossio, ${ }^{58 c}$ X. F. Cui, ${ }^{34}$ H. L. Dai, ${ }^{1,43}$ J. P. Dai, ${ }^{38, h}$ X. C. Dai, ${ }^{1,47}$ A. Dbeyssi, ${ }^{15}$ D. Dedovich,,${ }^{27}$ Z. Y. Deng, ${ }^{1}$ A. Denig, ${ }^{26}$ I. Denysenko, ${ }^{27}$ M. Destefanis, ${ }^{58 a, 58 c}$ F. De Mori, ${ }^{58 a, 58 c}$ Y. Ding, ${ }^{31}$ C. Dong, ${ }^{34}$ J. Dong, ${ }^{1,43}$ L. Y. Dong, ${ }^{1,47}$ M. Y. Dong, ${ }^{1,43,47}$ Z. L. Dou, ${ }^{33}$ S. X. Du, ${ }^{63}$ J. Z. Fan, ${ }^{45}$ J. Fang, ${ }^{1,43}$ S. S. Fang, ${ }^{1,47}$ Y. Fang, ${ }^{1}$ R. Farinelli, ${ }^{24 a, 24 b}$ L. Fava, ${ }^{58 b, 58 c}$ F. Feldbauer, ${ }^{4}$ G. Felici, ${ }^{23 a}$ C. Q. Feng, ${ }^{55,43}$ M. Fritsch, ${ }^{4}$ C. D. Fu, ${ }^{1}$ Y. Fu, ${ }^{1}$ Q. Gao, ${ }^{1}$ X. L. Gao, ${ }^{55,43}$ Y. Gao, ${ }^{56}$ Y. Gao, ${ }^{45}$ Y. G. Gao, ${ }^{6}$ Z. Gao, ${ }^{55,43}$ B. Garillon, ${ }^{26}$ I. Garzia, ${ }^{24 a}$ E. M. Gersabeck, ${ }^{50}$ A. Gilman, ${ }^{51}$ K. Goetzen, ${ }^{11}$ L. Gong, ${ }^{34}$ W. X. Gong, ${ }^{1,43}$ W. Gradl, ${ }^{26}$
M. Greco, ${ }^{58 \mathrm{a}, 58 \mathrm{c}}$ L. M. Gu, ${ }^{33}$ M. H. Gu, ${ }^{1,43}$ S. Gu, ${ }^{2}$ Y. T. Gu, ${ }^{13}$ A. Q. Guo, ${ }^{22}$ L. B. Guo, ${ }^{32}$ R. P. Guo, ${ }^{36}$ Y. P. Guo, ${ }^{26}$ A. Guskov, ${ }^{27}$ S. Han, ${ }^{60}$ X. Q. Hao, ${ }^{16}$ F. A. Harris, ${ }^{48}$ K. L. He, ${ }^{1,47}$ F. H. Heinsius, ${ }^{4}$ T. Held, ${ }^{4}$ Y. K. Heng, ${ }^{1,43,47}$ Y. R. Hou, ${ }^{47}$ Z. L. Hou, ${ }^{1}$ H. M. Hu, ${ }^{1,47}$ J. F. Hu, ${ }^{38, h}$ T. Hu, ${ }^{1,43,47}$ Y. Hu, ${ }^{1}$ G. S. Huang, ${ }^{55,43}$ J. S. Huang, ${ }^{16}$ X. T. Huang, ${ }^{37}$ X. Z. Huang, ${ }^{33}$ N. Huesken, ${ }^{52}$ T. Hussain, ${ }^{57}$ W. Ikegami Andersson, ${ }^{59}$ W. Imoehl, ${ }^{22}$ M. Irshad, ${ }^{55,43}$ Q. Ji, ${ }^{1}$ Q. P. Ji, ${ }^{16}$ X. B. Ji, ${ }^{1,47}$ X. L. Ji, ${ }^{1,43}$ H. L. Jiang, ${ }^{37}$ X. S. Jiang, ${ }^{1,43,47}$ X. Y. Jiang, ${ }^{34}$ J. B. Jiao, ${ }^{37}$ Z. Jiao, ${ }^{18}$ D. P. Jin, ${ }^{1,43,47}$ S. Jin, ${ }^{33}$ Y. Jin, ${ }^{49}$ T. Johansson, ${ }^{59}$
N. Kalantar-Nayestanaki, ${ }^{29}$ X. S. Kang, ${ }^{31}$ R. Kappert, ${ }^{29}$ M. Kavatsyuk, ${ }^{29}$ B. C. Ke, ${ }^{1}$ I. K. Keshk, ${ }^{4}$ T. Khan, ${ }^{55,43}$ A. Khoukaz, ${ }^{52}$ P. Kiese, ${ }^{26}$ R. Kiuchi, ${ }^{1}$ R. Kliemt, ${ }^{11}$ L. Koch, ${ }^{28}$ O. B. Kolcu, ${ }^{46 b, f}$ B. Kopf, ${ }^{4}$ M. Kuemmel, ${ }^{4}$ M. Kuessner, ${ }^{4}$ A. Kupsc, ${ }^{59}$ M. Kurth, ${ }^{1}$ M. G. Kurth, ${ }^{1,47}$ W. Kühn, ${ }^{28}$ J. S. Lange, ${ }^{28}$ P. Larin, ${ }^{15}$ L. Lavezzi, ${ }^{58 c}$ H. Leithoff, ${ }^{26}$ T. Lenz, ${ }^{26}$ C. Li, ${ }^{59}$
 P. L. Li ${ }^{55,43}$ P. R. Li, ${ }^{30}$ Q. Y. Li, ${ }^{37}$ W. D. Li, ${ }^{1,47}$ W. G. Li, ${ }^{1}$ X. H. Li, ${ }^{55,43}$ X. L. Li,${ }^{37}$ X. N. Li, ${ }^{1,43}$ X. Q. Li ${ }^{34}{ }^{34}$ Z. B. Li, ${ }^{44}$ Z. Y. Li, ${ }^{44}$ H. Liang, ${ }^{1,47}$ H. Liang, ${ }^{55,43}$ Y. F. Liang, ${ }^{40}$ Y. T. Liang, ${ }^{28}$ G. R. Liao, ${ }^{12}$ L. Z. Liao, ${ }^{1,47}$ J. Libby, ${ }^{21}$ C. X. Lin, ${ }^{44}$ D. X. Lin, ${ }^{15}$ Y. J. Lin, ${ }^{13}$ B. Liu, ${ }^{38, h}$ B. J. Liu, ${ }^{1}$ C. X. Liu, ${ }^{1}$ D. Liu, ${ }^{55,43}$ D. Y. Liu, ${ }^{38, h}$ F. H. Liu, ${ }^{39}$ Fang Liu, ${ }^{1}$ Feng Liu, ${ }^{6}$ H. B. Liu, ${ }^{13}$ H. M. Liu, ${ }^{1,47}$ Huanhuan Liu, ${ }^{1}$ Huihui Liu, ${ }^{17}$ J. B. Liu, ${ }^{55,43}$ J. Y. Liu, ${ }^{1,47}$ K. Y. Liu, ${ }^{31}$ Ke Liu, ${ }^{6}$ Q. Liu, ${ }^{47}$ S. B. Liu, ${ }^{55,43}$ T. Liu, ${ }^{1,47}$ X. Liu, ${ }^{30}$ X. Y. Liu, ${ }^{1,47}$ Y. B. Liu, ${ }^{34}$ Z. A. Liu, ${ }^{1,43,47}$ Zhiqing Liu, ${ }^{37}$ Y. F. Long, ${ }^{35}$ X. C. Lou, ${ }^{1,43,47}$ H. J. Lu, ${ }^{18}$ J. D. Lu, ${ }^{1,47}$ J. G. Lu, ${ }^{1,43}$ Y. Lu, ${ }^{1}$ Y. P. Lu, ${ }^{1,43}$ C. L. Luo, ${ }^{32}$ M. X. Luo, ${ }^{62}$ P. W. Luo, ${ }^{44}$ T. Luo, ${ }^{9, j}$ X. L. Luo, ${ }^{1,43}$ S. Lusso, ${ }^{58 c}$ X. R. Lyu, ${ }^{47}$ F. C. Ma, ${ }^{31}$ H. L. Ma, ${ }^{1}$ L.L. Ma, ${ }^{37}$ M. M. Ma, ${ }^{1,47}$ Q. M. Ma, ${ }^{1}$ X. N. Ma, ${ }^{34}$ X. X. Ma, ${ }^{1,47}$ X. Y. Ma, ${ }^{1,43}$ Y. M. Ma, ${ }^{37}$ F. E. Maas, ${ }^{15}$ M. Maggiora, ${ }^{58 a, 58 c}$ S. Maldaner, ${ }^{26}$ S. Malde, ${ }^{53}$ Q. A. Malik, ${ }^{57}$ A. Mangoni, ${ }^{23 b}$ Y. J. Mao, ${ }^{35}$ Z. P. Mao, ${ }^{1}$ S. Marcello, ${ }^{58 a, 58 \mathrm{c}}$ Z. X. Meng, ${ }^{49}$ J. G. Messchendorp, ${ }^{29}$ G. Mezzadri, ${ }^{24 \mathrm{a}}$ J. Min, ${ }^{1,43}$ T. J. Min, ${ }^{33}$ R. E. Mitchell, ${ }^{22}$ X. H. Mo, ${ }^{1,43,47}$ Y. J. Mo, ${ }^{6}$ C. Morales Morales, ${ }^{15}$ N. Yu. Muchnoi, ${ }^{10, \mathrm{~d}}$ H. Muramatsu, ${ }^{51}$ A. Mustafa, ${ }^{4}$ S. Nakhoul, ${ }^{11, g}$ Y. Nefedov,${ }^{27}$ F. Nerling, ${ }^{11, g}$ I. B. Nikolaev, ${ }^{10, \mathrm{~d}}$ Z. Ning, ${ }^{1,43}$ S. Nisar, ${ }^{8, k}$ S. L. Niu, ${ }^{1,43}$ S. L. Olsen, ${ }^{47}$ Q. Ouyang, ${ }^{1,43,47}$ S. Pacetti, ${ }^{23 b}$ Y. Pan, ${ }^{55,43}$ M. Papenbrock, ${ }^{59}$ P. Patteri, ${ }^{23 a}$ M. Pelizaeus, ${ }^{4}$ H. P. Peng, ${ }^{55,43}$ K. Peters, ${ }^{11, g}$ J. Pettersson, ${ }^{59}$ J. L. Ping, ${ }^{32}$ R. G. Ping, ${ }^{1,47}$ A. Pitka, ${ }^{4}$ R. Poling, ${ }^{51}$ V. Prasad, ${ }^{55,43}$ M. Qi, ${ }^{33}$ T. Y. Qi, ${ }^{2}$ S. Qian, ${ }^{1,43}$ C. F. Qiao, ${ }^{47}$ N. Qin, ${ }^{60}$ X. P. Qin, ${ }^{13}$ X. S. Qin, ${ }^{4}$ Z. H. Qin, ${ }^{1,43}$ J. F. Qiu, ${ }^{1}$ S. Q. Qu, ${ }^{34}$ K. H. Rashid, ${ }^{57, i}$ K. Ravindran, ${ }^{21}$ C. F. Redmer ${ }^{26}$ M. Richter, ${ }^{4}$ M. Ripka, ${ }^{26}$ A. Rivetti, ${ }^{58 c}$ V. Rodin, ${ }^{29}$ M. Rolo, ${ }^{58 c}$ G. Rong, ${ }^{1,47}$ Ch. Rosner, ${ }^{15}$ M. Rump, ${ }^{52}$ A. Sarantsev, ${ }^{27, e}$ M. Savri, ${ }^{24 b}$ K. Schoenning, ${ }^{59}$ W. Shan, ${ }^{19}$ X. Y. Shan, ${ }^{55,43}$ M. Shao, ${ }^{55,43}$ C. P. Shen, ${ }^{2}$ P. X. Shen, ${ }^{34}$ X. Y. Shen, ${ }^{1,47}$ H. Y. Sheng, ${ }^{1}$ X. Shi, ${ }^{1,43}$ X. D. Shi, ${ }^{55,43}$ J. J. Song, ${ }^{37}$ Q. Q. Song, ${ }^{55,43}$ X. Y. Song, ${ }^{1}$ S. Sosio, ${ }^{58 a, 58 c}{ }^{5}$ C. Sowa, ${ }^{4}$ S. Spataro, ${ }^{58 a, 58 \mathrm{c}}$ F. F. Sui, ${ }^{37}$ G. X. Sun, ${ }^{1}$ J. F. Sun, ${ }^{16}$ L. Sun, ${ }^{60}$ S. S. Sun, ${ }^{1,47}$ X. H. Sun, ${ }^{1}$ Y. J. Sun,${ }^{55,43}$ Y. K. Sun,${ }^{55,43}$ Y. Z. Sun, ${ }^{1}$ Z. J. Sun, ${ }^{1,43}$ Z. T. Sun, ${ }^{1}$ Y. T. Tan, ${ }^{55,43}$ C. J. Tang, ${ }^{40}$ G. Y. Tang, ${ }^{1}$ X. Tang, ${ }^{1}$ V. Thoren, ${ }^{59}$ B. Tsednee, ${ }^{25}$ I. Uman, ${ }^{46 \mathrm{~d}}$ B. Wang, ${ }^{1}$
B. L. Wang, ${ }^{47}$ C. W. Wang, ${ }^{33}$ D. Y. Wang, ${ }^{35}$ H. H. Wang, ${ }^{37}$ K. Wang, ${ }_{55}^{1,43}$ L. L. Wang, ${ }^{1}$ L. S. Wang, ${ }^{1}$ M. Wang, ${ }^{37}$ M. Z. Wang, ${ }^{35}$ Meng Wang, ${ }^{1,47}$ P. L. Wang, ${ }^{1}$ R. M. Wang, ${ }^{61}$ W. P. Wang, ${ }^{55,43}$ X. Wang, ${ }^{35}$ X. F. Wang, ${ }^{1}$ X. L. Wang, ${ }^{9, j}$ Y. Wang, ${ }^{44}$ Y. Wang, ${ }^{55,43}$ Y. F. Wang, ${ }^{1,43,47}$ Z. Wang, ${ }^{1,43}$ Z. G. Wang, ${ }^{1,43}$ Z. Y. Wang, ${ }^{1}$ Zongyuan Wang, ${ }^{1,47}$ T. Weber, ${ }^{4}$ D. H. Wei, ${ }^{12}$ P. Weidenkaff, ${ }^{26}$ H. W. Wen, ${ }^{32}$ S. P. Wen, ${ }^{1}$ U. Wiedner, ${ }^{4}$ G. Wilkinson, ${ }^{53}$ M. Wolke, ${ }^{59}$ L. H. Wu, ${ }^{1}$ L. J. Wu, ${ }^{1,47}$
Z. Wu, ${ }^{1,43}$ L. Xia, ${ }^{55,43}$ Y. Xia, ${ }^{20}$ S. Y. Xiao, ${ }^{1}$ Y. J. Xiao, ${ }^{1,47}$ Z. J. Xiao, ${ }^{32}$ Y. G. Xie, ${ }^{1,43}$ Y. H. Xie, ${ }^{6}$ T. Y. Xing, ${ }^{1,47}$ X. A. Xiong, ${ }^{1,47}$ Q. L. Xiu, ${ }^{1,43}$ G.F. Xu, ${ }^{1}$ J. J. Xu, ${ }^{33}$ L. Xu, ${ }^{1}$ Q. J. Xu, ${ }^{14}$ W. Xu, ${ }^{1,47}$ X. P. Xu, ${ }^{41}$ F. Yan, ${ }^{56}$ L. Yan, ${ }^{58 a, 58 c}$ W. B. Yan, ${ }^{55,43}$ W. C. Yan, ${ }^{2}$ Y. H. Yan, ${ }^{20}$ H. J. Yang, ${ }^{38, h}$ H. X. Yang, ${ }^{1}$ L. Yang, ${ }^{60}$ R. X. Yang, ${ }^{55,43}$ S. L. Yang, ${ }^{1,47}$ Y. H. Yang, ${ }^{33}$ Y. X. Yang, ${ }^{12}$ Yifan Yang, ${ }^{1,47}$ Z. Q. Yang, ${ }^{20}$ M. Ye, ${ }^{1,43}$ M. H. Ye, ${ }^{7}$ J. H. Yin, ${ }^{1}$ Z. Y. You, ${ }^{44}$ B. X. Yu, ${ }^{1,43,47}$ C. X. Yu, ${ }^{34}$ J. S. Yu, ${ }^{20}$ C. Z. Yuan, ${ }^{1,47}$ X. Q. Yuan, ${ }^{35}$ Y. Yuan, ${ }^{1}$ A. Yuncu, ${ }^{46 b, a}$ A. A. Zafar, ${ }^{57}$ Y. Zeng, ${ }^{20}$ B. X. Zhang, ${ }^{1}$ B. Y. Zhang, ${ }^{1,43}$ C. C. Zhang, ${ }^{1}$ D. H. Zhang, ${ }^{1}$ H. H. Zhang, ${ }^{44}$ H. Y. Zhang, ${ }^{1,43}$ J. Zhang, ${ }^{1,47}$ J. L. Zhang, ${ }^{61}$ J. Q. Zhang, ${ }^{4}$ J. W. Zhang, ${ }^{1,43,47}$ J. Y. Zhang, ${ }^{1}$ J. Z. Zhang, ${ }^{1,47}$ K. Zhang, ${ }^{1,47}$ L. Zhang, ${ }^{45}$ S. F. Zhang, ${ }^{33}$ T. J. Zhang, ${ }^{38, h}$ X. Y. Zhang, ${ }^{37}$ Y. Zhang, ${ }^{55,43}$
Y. H. Zhang, ${ }^{1,43}$ Y. T. Zhang, ${ }^{55,43}$ Yang Zhang, ${ }^{1}$ Yao Zhang, ${ }^{1}$ Yi Zhang, ${ }^{9, j}$ Yu Zhang, ${ }^{47}$ Z. H. Zhang, ${ }^{6}$ Z. P. Zhang, ${ }^{55}$ Z. Y. Zhang, ${ }^{60}$ G. Zhao, ${ }^{1}$ J. W. Zhao, ${ }^{1,43}$ J. Y. Zhao, ${ }^{1,47}$ J. Z. Zhao, ${ }^{1,43}$ Lei Zhao, ${ }^{55,43}$ Ling Zhao, ${ }^{1}$ M. G. Zhao, ${ }^{34}$ Q. Zhao, ${ }^{1}$
S. J. Zhao, ${ }^{63}$ T. C. Zhao, ${ }^{1}$ Y. B. Zhao, ${ }^{1,43}$ Z. G. Zhao, ${ }^{55,43}$ A. Zhemchugov, ${ }^{27, b}$ B. Zheng, ${ }^{56}$ J. P. Zheng, ${ }^{1,43}$ Y. Zheng, ${ }^{35}$ Y. H. Zheng, ${ }^{47}$ B. Zhong, ${ }^{32}$ L. Zhou, ${ }^{1,43}$ L. P. Zhou, ${ }^{1,47}$ Q. Zhou, ${ }^{1,47,{ }^{*}}$ X. Zhou, ${ }^{60}$ X. K. Zhou, ${ }^{47}$ X. R. Zhou, ${ }^{55,43}$ Xiaoyu Zhou, ${ }^{20}$ Xu Zhou, ${ }^{20}$ A. N. Zhu, ${ }^{1,47}$ J. Zhu, ${ }^{34}$ J. Zhu, ${ }^{44}$ K. Zhu, ${ }^{1}$ K. J. Zhu, ${ }^{1,43,47}$ S. H. Zhu, ${ }^{54}$ W. J. Zhu, ${ }^{34}$ X. L. Zhu, ${ }^{45}$ Y. C. Zhu, ${ }^{55,43}$ Y. S. Zhu, ${ }^{1,47}$ Z. A. Zhu, ${ }^{1,47}$ J. Zhuang, ${ }^{1,43}$ B. S. Zou, ${ }^{1}$ and J. H. Zou ${ }^{1}$

## (BESIII Collaboration)

${ }^{1}$ Institute of High Energy Physics, Beijing 100049, People's Republic of China
${ }^{2}$ Beihang University, Beijing 100191, People's Republic of China
${ }^{3}$ Beijing Institute of Petrochemical Technology, Beijing 102617, People's Republic of China
${ }^{4}$ Bochum Ruhr-University, D-44780 Bochum, Germany
${ }^{5}$ Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA
${ }^{6}$ Central China Normal University, Wuhan 430079, People's Republic of China
${ }^{7}$ China Center of Advanced Science and Technology, Beijing 100190, People's Republic of China
${ }^{8}$ COMSATS University Islamabad, Lahore Campus, Defence Road, Off Raiwind Road, 54000 Lahore, Pakistan
${ }^{9}$ Fudan University, Shanghai 200443, People's Republic of China
${ }^{10}$ G.I. Budker Institute of Nuclear Physics SB RAS (BINP), Novosibirsk 630090, Russia
${ }^{11}$ GSI Helmholtzcentre for Heavy Ion Research GmbH, D-64291 Darmstadt, Germany
${ }^{12}$ Guangxi Normal University, Guilin 541004, People's Republic of China
${ }^{13}$ Guangxi University, Nanning 530004, People's Republic of China
${ }^{14}$ Hangzhou Normal University, Hangzhou 310036, People's Republic of China
${ }^{15}$ Helmholtz Institute Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany
${ }^{16}$ Henan Normal University, Xinxiang 453007, People's Republic of China
${ }^{17}$ Henan University of Science and Technology, Luoyang 471003, People's Republic of China
${ }^{18}$ Huangshan College, Huangshan 245000, People's Republic of China
${ }^{19}$ Hunan Normal University, Changsha 410081, People's Republic of China
${ }^{20}$ Hunan University, Changsha 410082, People's Republic of China
${ }^{21}$ Indian Institute of Technology Madras, Chennai 600036, India
${ }^{22}$ Indiana University, Bloomington, Indiana 47405, USA
${ }^{23 a}$ INFN Laboratori Nazionali di Frascati, I-00044, Frascati, Italy
${ }^{23 \mathrm{~b}}$ INFN and University of Perugia, I-06100, Perugia, Italy ${ }^{24 a}$ INFN Sezione di Ferrara, I-44122, Ferrara, Italy
${ }^{24 \mathrm{~b}}$ University of Ferrara, I-44122, Ferrara, Italy
${ }^{25}$ Institute of Physics and Technology, Peace Ave. 54B, Ulaanbaatar 13330, Mongolia
${ }^{26}$ Johannes Gutenberg University of Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany
${ }^{27}$ Joint Institute for Nuclear Research, 141980 Dubna, Moscow region, Russia
${ }^{28}$ Justus-Liebig-Universitaet Giessen, II. Physikalisches Institut, Heinrich-Buff-Ring 16, D-35392 Giessen, Germany
${ }^{29}$ KVI-CART, University of Groningen, NL-9747 AA Groningen, The Netherlands
${ }^{30}$ Lanzhou University, Lanzhou 730000, People's Republic of China
${ }^{31}$ Liaoning University, Shenyang 110036, People's Republic of China
${ }^{32}$ Nanjing Normal University, Nanjing 210023, People's Republic of China
${ }^{33}$ Nanjing University, Nanjing 210093, People's Republic of China
${ }^{34}$ Nankai University, Tianjin 300071, People's Republic of China
${ }^{35}$ Peking University, Beijing 100871, People's Republic of China
${ }^{36}$ Shandong Normal University, Jinan 250014, People's Republic of China
${ }^{37}$ Shandong University, Jinan 250100, People's Republic of China
${ }^{38}$ Shanghai Jiao Tong University, Shanghai 200240, People's Republic of China
${ }^{39}$ Shanxi University, Taiyuan 030006, People's Republic of China
${ }^{40}$ Sichuan University, Chengdu 610064, People's Republic of China
${ }^{41}$ Soochow University, Suzhou 215006, People's Republic of China
${ }^{42}$ Southeast University, Nanjing 211100, People's Republic of China
${ }^{43}$ State Key Laboratory of Particle Detection and Electronics, Beijing 100049, Hefei 230026, People's Republic of China
${ }^{44}$ Sun Yat-Sen University, Guangzhou 510275, People's Republic of China
${ }^{45}$ Tsinghua University, Beijing 100084, People's Republic of China
${ }^{46 \mathrm{a}}$ Ankara University, 06100 Tandogan, Ankara, Turkey
${ }^{46 \mathrm{~b}}$ Istanbul Bilgi University, 34060 Eyup, Istanbul, Turkey
${ }^{46 \mathrm{c}}$ Uludag University, 16059 Bursa, Turkey

${ }^{46 \mathrm{~d}}$ Near East University, Nicosia, North Cyprus, Mersin 10, Turkey<br>${ }^{47}$ University of Chinese Academy of Sciences, Beijing 100049, People's Republic of China<br>${ }^{48}$ University of Hawaii, Honolulu, Hawaii 96822, USA<br>${ }^{49}$ University of Jinan, Jinan 250022, People's Republic of China<br>${ }^{50}$ University of Manchester, Oxford Road, Manchester, M13 9PL, United Kingdom<br>${ }^{51}$ University of Minnesota, Minneapolis, Minnesota 55455, USA<br>${ }^{52}$ University of Muenster, Wilhelm-Klemm-Str. 9, 48149 Muenster, Germany<br>${ }^{53}$ University of Oxford, Keble Rd, Oxford, UK OX13RH<br>${ }^{54}$ University of Science and Technology Liaoning, Anshan 114051, People's Republic of China<br>${ }^{55}$ University of Science and Technology of China, Hefei 230026, People's Republic of China<br>${ }^{56}$ University of South China, Hengyang 421001, People's Republic of China<br>${ }^{57}$ University of the Punjab, Lahore-54590, Pakistan<br>${ }^{58 a}$ University of Turin, I-10125, Turin, Italy<br>${ }^{58 \mathrm{~b}}$ University of Eastern Piedmont, I-15121, Alessandria, Italy<br>${ }^{58 \mathrm{c}}$ INFN, I-10125, Turin, Italy<br>${ }^{59}$ Uppsala University, Box 516, SE-75120 Uppsala, Sweden<br>${ }^{60}$ Wuhan University, Wuhan 430072, People's Republic of China<br>${ }^{61}$ Xinyang Normal University, Xinyang 464000, People's Republic of China<br>${ }^{62}$ Zhejiang University, Hangzhou 310027, People's Republic of China<br>${ }^{63}$ Zhengzhou University, Zhengzhou 450001, People's Republic of China

(Received 9 August 2019; published 19 September 2019)
Based on the data sample of $448.1 \times 10^{6} \psi(3686)$ events collected with the BESIII detector at BEPCII, we present a study of the decays $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda+$ c.c. and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda+$ c.c. The branching fractions of $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda+$ c.c. $(J=0,1,2)$ are measured to be $(4.8 \pm 0.7 \pm 0.5) \times 10^{-4}$, $(5.0 \pm 0.5 \pm 0.4) \times 10^{-4}$, and $(8.2 \pm 0.9 \pm 0.7) \times 10^{-4}$, respectively, where the first uncertainties are statistical and the second systematic. The branching fraction of $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda+$ c.c. is measured to be $(6.3 \pm 0.5 \pm 0.5) \times 10^{-5}$. All these decay modes are observed for the first time.

DOI: 10.1103/PhysRevD.100.052010

[^0]
## I. INTRODUCTION

The quark model provides a good description of both the ground states and some excited states of baryons. However, several resonances that are predicted by this model have not yet been observed, and hence there is an intense experimental effort underway to find these missing states [1]. The baryon coupling in conventional production channels (e.g., $\gamma$-nucleon) can be quite small, but the coupling between baryons and $\chi_{c J}$ decays via $g g$ gluons could be larger (e.g., $\psi$ or $\chi_{c J}$ decays). For this reason, charmonium decay is a promising process to study excited nucleons and hyperons [2].

The BES Collaboration has reported a study of $J / \psi \rightarrow$ $\bar{p} K^{+} \Lambda+$ c.c. and $\psi(3686) \rightarrow \bar{p} K^{+} \Lambda+$ c.c. decays [3], in which a threshold enhancement in the $\bar{p} \Lambda$ mass spectrum was observed. Throughout this paper, the inclusion of charge conjugate channels is implied. The BESIII Collaboration also reported a study of $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \Lambda$ [4], where a near threshold enhancement in the mass spectrum of $\bar{p} \Lambda$ was observed in $\chi_{c 0}$ decay. This enhancement may be interpreted as a quasibound dibaryon state, or as an enhancement due to final-state interaction, or simply as an interference effect of high-mass $N^{*}$ and $\Lambda^{*}$ states [4]. The study of the resonant structures in the similar decay modes
$\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$ may help in the understanding of the $\bar{p} \Lambda$ threshold structure.

Until now, no experimental results exist concerning the decays $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ and $\psi(3686) \rightarrow$ $\bar{p} K^{*+} \Lambda$. In this analysis, the branching fractions (BFs) of $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda(J=0,1,2)$ and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$ are measured for the first time with a data sample of $448.1 \times$ $10^{6} \psi(3686)$ events [5]. Moreover, possible substructures in invariant mass spectra of $\bar{p} K^{*+}, K^{*+} \Lambda$, and $\bar{p} \Lambda$ are investigated.

## II. BESIII DETECTOR AND MONTE CARLO SIMULATION

The Beijing Electron Positron Collider II (BEPCII) is a double-ring $e^{+} e^{-}$collider running at center-of-mass energy ranging from 2.0 to 4.6 GeV . The BESIII detector [6] at BEPCII, with a geometrical acceptance of $93 \%$ of the $4 \pi$ solid angle, operates in a magnetic filed of 1.0 T provided by a superconducting solenoid magnet. The detector is composed of a helium-based main drift chamber (MDC), a plastic-scintillator time-of-flight (TOF) system, a $\mathrm{CsI}(\mathrm{Tl})$ electromagnetic calorimeter (EMC) and a resistive plate chambers (RPC)-based muon chamber (MUC). The spatial resolution of the MDC is better than $130 \mu \mathrm{~m}$, the charged track momentum resolution is $0.5 \%$ at $1 \mathrm{GeV} / c$, and the energy-loss $(d E / d x)$ resolution is better than $6 \%$ for electrons from Bhabha events. The time resolution of the TOF is $80 \mathrm{ps}(110 \mathrm{ps})$ in the barrel (endcaps. The energy resolution of the EMC at 1.0 GeV is $2.5 \% ~(5 \%)$ in the barrel (endcaps). The position resolution in the MUC is better than 2 cm .

Simulated Monte Carlo (MC) events are used to determine the detection efficiency, optimize selection criteria and estimate the level of contamination from background processes. The GEANT 4-based [7] simulation package bOOST includes a geometric and material description of the BESIII detector, detector response, and digitization models, and also tracks the running conditions and performance of the detector. The production of $\psi(3686)$ events is simulated with KKMC [8], where the known decay modes are generated by EVTGEN $[9,10]$ with their BFs taken from the Particle Data Group (PDG) [11], and the remaining unknown decays are generated by LundCHARM [12]. Exclusive MC samples of $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$ are generated to determine detection efficiencies. In the signal MC simulation, the angular distribution of the decay $\psi(3686) \rightarrow \gamma \chi_{c J}$ has the form $1+$ $\alpha \cos ^{2} \theta$ with $\alpha=1,-1 / 3,1 / 13$ for $J=0,1,2$, respectively, where $\theta$ is the photon polar angle [13]. The weak decay of $\Lambda$ is generated with a model that includes parity violation. Other relevant decays are generated with BESEVTGEN [10] with a uniform distribution in phase space.

## III. ANALYSIS OF $\psi(\mathbf{3 6 8 6}) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \boldsymbol{\Lambda}$

## A. Event selection

The process $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ is reconstructed with $\Lambda \rightarrow p \pi^{-}, K^{*+} \rightarrow K^{+} \pi^{0}$, and $\pi^{0} \rightarrow \gamma \gamma$. Events are required to have at least two positive and two negative charged tracks. For each charged track, the polar angle in the MDC must satisfy $|\cos \theta|<0.93$. The combined TOF and $d E / d x$ information is used to form particle identification (PID) confidence levels for pion, kaon and proton hypotheses. Each track is assigned to the particle hypothesis with the highest confidence level. The identified $\bar{p}$ and $K^{+}$candidates are further required to have their point of closest approach to the interaction point (IP) within $\pm 1 \mathrm{~cm}$ in the plane perpendicular to beam direction and within $\pm 10 \mathrm{~cm}$ in the plane of the beam direction. A common vertex constraint is applied to all $p \pi^{-}$pairs assumed to arise from a $\Lambda$ decay, and the production of the $\Lambda$ candidates is constrained to be at the interaction point. Only $d E / d x$ information is used for the PID of $p$ and $\pi^{-}$ candidates in $\Lambda$ decays, because many of these particles do not reach the TOF on account of their low momentum.

Photon candidates are required to have energy deposition greater than 25 MeV in the barrel $\mathrm{EMC}(|\cos \theta|<0.8)$ and 50 MeV in the end cap EMC $(0.86<|\cos \theta|<0.92)$. To exclude showers from charged tracks, the angle between the direction of the photon and the nearest charged track is required to be greater than $5^{\circ}$. In addition, the angle between the direction of the photon and antiproton is required to be greater than $10^{\circ}$ to suppress background from anti-proton annihilation in the detector. The measured EMC time is required to be within 0 and 700 ns of start time of the event to suppress electronic noise and any energy deposition unrelated to the event.

To improve the mass resolution, the selected photons, antiproton, kaon, and $\Lambda$ candidate are subjected to a five-constraint (5C) kinematic fit under the hypothesis of $\psi(3686) \rightarrow$ $\gamma \bar{p} K^{+} \pi^{0} \Lambda$ with the invariant mass of the two photons being constrained to the $\pi^{0}$ mass. The $\chi^{2}$ of the 5C fit is required to be less than 70 . For events with more than one combination satisfying this requirement, only the combination with the smallest $\chi^{2}$ is accepted. To veto background events from $\psi(3686) \rightarrow \bar{p} K^{+} \pi^{0} \Lambda$ and $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \Lambda$, an alternative $5 \mathrm{C}(4 \mathrm{C})$ kinematic fit is performed under the hypotheses of $\psi(3686) \rightarrow \bar{p} K^{+} \pi^{0} \Lambda\left(\gamma \bar{p} K^{+} \Lambda\right)$. We further require the confidence level of the kinematic fit for the $\psi(3686) \rightarrow \bar{p} K^{+} \pi^{0} \Lambda$ assignment to be larger than those for the $\psi(3686) \rightarrow$ $\gamma \bar{p} K^{+} \pi^{0} \Lambda$ and $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \Lambda$ hypotheses.

The $K^{+} \pi^{0}$ invariant mass distribution is shown in Fig. 1(a), where an obvious $K^{*+}$ structure can be seen. The $K^{*+}$ candidates are selected by requiring $\mid M_{K^{+} \pi^{0}}-$ $M_{K^{*+}} \mid<0.1 \mathrm{GeV} / c^{2}$, where $M_{K^{*+}}$ is the nominal mass of the $K^{*+}$ meson [11]. The $K^{*+}$ sidebands, also indicated in Fig. 1(a), are chosen to be $1.1<M_{K^{+} \pi^{0}}<1.2 \mathrm{GeV} / c^{2}$ and $0.65<M_{K^{+} \pi^{0}}<0.75 \mathrm{GeV} / c^{2}$. Figure 1 (b) shows the


FIG. 1. Invariant mass distribution of (a) $K^{+} \pi^{0}$ and (b) $p \pi^{-}$. The solid arrows indicate the mass windows used as the selection criteria in the analysis. The dashed arrows indicate the sidebands region.


FIG. 2. Invariant mass spectrum of $\bar{p} K^{*+} \Lambda$. The three arrowpairs indicate, from left to right, the mass windows for $\chi_{c 0}, \chi_{c 1}$, and $\chi_{c 2}$, respectively.
$M_{p \pi^{-}}$distribution, from which $\Lambda$ candidates are selected by requiring $\left|M_{p \pi^{-}}-M_{\Lambda}\right|<6 \mathrm{MeV} / c^{2}$, where $M_{\Lambda}$ is the nominal $\Lambda$ mass [11]. Background events from $\psi(3686) \rightarrow$ $J / \psi \pi^{0} \pi^{0}, \quad J / \psi \rightarrow \bar{p} K^{+} \Lambda$ are rejected by requiring $\left|M_{\bar{p} K^{+} \Lambda}-M_{J / \psi}\right|>0.05 \mathrm{GeV} / c^{2}$, where $M_{J / \psi}$ is the nominal $J / \psi$ mass [11]. To remove the background from the cascade decay $\psi(3686) \rightarrow \bar{p} K^{+} \Sigma^{0}, \Sigma^{0} \rightarrow \gamma \Lambda$, the additional selection requirement $M_{\gamma \Lambda}>1.21 \mathrm{GeV} / c^{2}$ is applied.

After applying these requirements, $\chi_{c J}$ signals are clearly seen in the invariant mass spectrum of $\bar{p} K^{*+} \Lambda$, as shown in Fig. 2. The mass windows used to select the $\chi_{c 0}, \chi_{c 1}, \chi_{c 2}$ candidates correspond to about three times the $\chi_{c J}$ width convolved with the mass resolution, which are $3.35-3.48,3.49-3.53$, and $3.53-3.59 \mathrm{GeV} / c^{2}$, respectively.

The invariant mass spectra of the $\bar{p} K^{*+}, \bar{p} \Lambda$, and $K^{*+} \Lambda$ combinations and the corresponding Dalitz plots are shown in Fig. 3 for each $\chi_{c J}$ state. No significant substructure is seen in the Dalitz plots of $\bar{p} K^{*+} \Lambda$ distributions. In order to search for the near-threshold structure of $M_{\bar{p} \Lambda}$ observed in Ref. [4] in the decay $\chi_{c 0} \rightarrow \bar{p} K^{+} \Lambda$, fits are performed on $M_{\bar{p} \Lambda}$ where the structure is described by a weighted BreitWigner resonance with parameters fixed to those reported in Ref. [4]. These fits return a statistical significance for the structure of $2.1 \sigma, 2.5 \sigma$, and $1.9 \sigma$ for the $\chi_{c 0}, \chi_{c 1}$, and $\chi_{c 2}$ states, respectively.

## B. Background study

Using an inclusive MC sample of $506 \times 10^{6} \psi(3686)$ events, the background from fake $\Lambda$ is found together with fake $K^{*+}$. So, the background can be categorized into the following four types: (1) events with a genuine $K^{*+}$ and a fake $\chi_{c J}\left(K^{*}\right.$, non- $\left.\chi_{c J}\right) ;(2)$ events with a genuine $\chi_{c J}$ and a fake $K^{*}\left(\chi_{c J}\right.$, non- $\left.K^{*}\right)$; (3) events with fake $K^{*}$ and $\chi_{c J}$ candidates (non- $K^{*}$, non- $\chi_{c J}$ ); (4) events containing a genuine $K^{*+}$ and a genuine $\chi_{c J}\left(K^{*}, \chi_{c J}\right)$. The contributions from the first three categories can be estimated by performing a two-dimensional (2-D) fit to the distribution of $M_{K^{+} \pi^{0}}$ versus $M_{\bar{p} K^{*+} \Lambda}$. The fourth type of background events come mainly from the processes $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow$ $\gamma \bar{p} K^{*+} \Lambda \rightarrow \gamma \gamma \bar{p} K^{+} \Lambda, \quad \psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda \rightarrow$ $\gamma \bar{p} K^{*+} \gamma p \pi^{-}, \psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \gamma J / \psi \rightarrow \gamma \gamma \bar{p} K^{*+} \Lambda$ and $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Sigma^{0}$. The first two of these contributions are negligible, on account of the low BF of radiative $K^{*+}$ and $\Lambda$ decays. The level of contamination coming from the other two modes is assessed by applying the selection to samples of exclusive MC events. For the normalization procedure, the BF of $\psi(3686) \rightarrow \gamma \chi_{c J}$, $\chi_{c J} \rightarrow \gamma J / \psi, J / \psi \rightarrow \bar{p} K^{*+} \Lambda$ is estimated to be less than $10^{-5}$, which implies negligible background of less than one event from this source. The normalized number of $\psi(3686) \rightarrow \gamma \chi_{c J}, \quad \chi_{c J} \rightarrow \bar{p} K^{*+} \Sigma^{0}$ background events is estimated to be $11.7 \pm 3.5,5.1 \pm 2.3,4.8 \pm 2.6$ for $\chi_{c J}$ ( $J=0,1,2$ ), where the relative BFs used to calculate these yields are estimated from dedicated studies with the same data sample.

To investigate possible background from continuum processes, the same selection criteria are applied to a data


FIG. 3. The Dalitz plots of $\bar{p} K^{*+} \Lambda$ for $\chi_{c 0}$ (a), $\chi_{c 1}$ (b), and $\chi_{c 2}$ (c).


FIG. 4. (a) Distribution of $M_{K^{+} \pi^{0}}$ versus $M_{\bar{p} K^{*+} \Lambda}$ from data. The three boxes indicate from left to right the signal region of $\chi_{c 0}, \chi_{c 1}$, and $\chi_{c 2}$, respectively. (b) 2-D histogram sampled from the composite PDF of the 2-D fit. (c) and (d) are projections of the 2-D fit on the distributions of $M_{K^{+} \pi^{0}}$ and $M_{\bar{p} K^{*+} \Lambda}$, respectively. The dots with error bars are data; the solid curves show the fitting result; the longdashed curves are $\left(K^{*+}, \chi_{c J}\right)$ signal; the short-dashed curves are ( $K^{*+}$, non- $\chi_{c J}$ ) background; the dot-dashed curves are $\left(\chi_{c J}\right.$, non- $K^{*+}$ ) background and the dotted curves are (non- $K^{*+}$, non- $\chi_{c J}$ ) background.
sample of $2.93 \mathrm{fb}^{-1}$ [14] collected at $\sqrt{s}=3.773 \mathrm{GeV}$. After normalizing to the integrated luminosity of the $\psi(3686)$ data sample, $20.1 \pm 4.1$ events survive and no peak is found in the mass spectrum of $M_{\bar{p} K^{*+} \Lambda}$. As a cross check the selection is also performed on a data sample of $44.5 \mathrm{pb}^{-1}$ collected at $\sqrt{s}=3.65 \mathrm{GeV}$. Only one event survives, which corresponds to 14 events when normalized to the integrated luminosity of the $\psi(3686)$ data sample, and is consistent with the result of the first study. In the BF measurement any continuum contribution is included in the other sources of nonpeaking background and the total is estimated by the 2-D fit described below.

## C. Branching fraction measurement of $\chi_{c J} \rightarrow \bar{p} \boldsymbol{K}^{*+} \boldsymbol{\Lambda}$

The distribution of $M_{K^{+} \pi^{0}}$ versus $M_{\bar{p} K^{*+} \Lambda}$ is shown in Fig. 4. An unbinned extended maximum-likelihood 2-D fit is performed on this distribution to determine the number of $\left(K^{*+}, \chi_{c J}\right)$ events. The composite probability density function (PDF) is constructed as follows:

$$
\begin{align*}
F= & N_{\text {sig }}^{\mathrm{obs}} \times\left(F_{\text {sig }}^{K^{*}} \cdot F_{\text {sig }}^{\chi_{c J}}\right)+N_{\mathrm{bkg}}^{\chi_{c J} \text {,non }-K^{*}} \times\left(F_{\mathrm{bkg}}^{\mathrm{non}-K^{*}} \cdot F_{\text {sig }}^{\chi_{c J}}\right) \\
& +N_{\mathrm{bkg}}^{K^{*}, \text { non }-\chi_{c J}} \times\left(F_{\mathrm{bkg}}^{\mathrm{non}-\chi_{c J}} \cdot F_{\text {sig }}^{K^{*}}\right) \\
& +N_{\mathrm{bkg}}^{\mathrm{non}-K^{*} \chi_{c J}} \times\left(F_{\mathrm{bkg}}^{\mathrm{non}-K^{*}} \cdot F_{\mathrm{bkg}}^{\mathrm{non}-\chi_{c J}}\right) . \tag{1}
\end{align*}
$$

Here, $N_{\text {sig }}^{\mathrm{obs}}, N_{\mathrm{bkg}}^{\chi_{c J}, \text { non }-K^{*}}, N_{\mathrm{bkg}}^{K^{*} \text {,non }-\chi_{c J}}$, and $N_{\mathrm{bkg}}^{\mathrm{non}-K^{*} \chi_{c J}}$ are the numbers of $\left(K^{*}, \chi_{c J}\right)$ signal events, $\left(\chi_{c J}\right.$, non- $\left.K^{*}\right)$, $\left(K^{*}\right.$, non$\chi_{c J}$ ), and (non- $K^{*}$, non- $\chi_{c J}$ ) background events, respectively.

The shape of the $K^{*+}$ resonance, $F_{\text {sig }}^{K^{*}}$, is described by a $P$-wave Breit-Wigner (BW) function [15] convolved with a double-Gaussian function $(D G)$ that accounts for detector resolution, the parameters of which are determined from MC simulation. The definition of $F_{\text {sig }}^{K^{*}}$ is

$$
\begin{equation*}
F_{\text {sig }}^{K^{*}}(s)=\frac{M \Gamma(s)}{\left(s^{2}-M^{2}\right)^{2}+M^{2} \Gamma(s)^{2}} \otimes D G(s) \tag{2}
\end{equation*}
$$

where $\Gamma(s)=\Gamma\left(\frac{M}{s}\right)^{2}\left(\frac{q}{q_{0}}\right)^{2 L+1}, s$ is the invariant mass of the $K^{+} \pi^{0}$ pair, $M$ and $\Gamma$ are the $K^{*+}$ mass and width [11], $q$ is the $K^{+}$momentum in the $K^{*+}$ rest frame, $q_{0}$ is the $q$ value at $s=M$, and $L=1$ is the relative orbital angular momentum of $K^{+} \pi^{0}$.

The background distribution of the fake $K^{*+}$ contribution, $F_{\mathrm{bkg}}^{\mathrm{non}-K^{*}}$, is described by truncated polynomial function $F_{\mathrm{bkg}}^{\mathrm{non}-K^{*}}(s)=\left(s-m_{t}\right)^{a} e^{-b s-c s^{2}}$ [15], where $m_{t}$ is the threshold mass for $K^{+} \pi^{0}$ and $a, b, c$ are free parameters.

The shape of the $\chi_{c J}$ signal is described by
$F_{\text {sig }}^{\chi_{c J}}=E_{\gamma}^{3} \cdot f\left(E_{\gamma}\right) \cdot B W(m) \cdot \frac{B_{l}(Q)}{B_{l}\left(Q_{0}\right)} \otimes G(m ; \mu, \sigma)$.
Here $E_{\gamma}^{3}$ is an E1 radiative-transition factor and $f\left(E_{\gamma}\right)=$ $\frac{E_{0}^{2}}{E_{\gamma} E_{0}+\left(E_{\gamma}-E_{0}\right)^{2}}$ is a damping factor [16], where $E_{\gamma}$ is the energy of the radiative photon in the $\psi(3686)$ rest frame and $E_{0}=\frac{M_{\psi(3686)}^{2}-M_{\chi_{C J}}^{2}}{2 M_{\psi(368)}^{2}}$. In the relativistic BW function
$B W(m)$, the mass and width of the $\chi_{c J}$ are fixed to the PDG [11] values. The Blatt-Weisskopf barrier factor [17] $B_{l}(Q)$ is a function of $Q$, which is the momentum of either the radiative photon or the $\chi_{c J}$ in the $\psi(3686)$ rest frame, $Q_{0}$ is the $Q$ value at $m=M_{\chi_{c I}}$, where $m$ is the invariant mass of the $\bar{p} K^{*+} \Lambda$ combination. Finally, $G(m ; \mu, \sigma)$ is a modified Gaussian function parametrizing the instrumental mass resolution, taking the form [18]

$$
\begin{equation*}
G(m ; \mu, \sigma)=\frac{1}{\sqrt{2 \pi} \sigma} e^{-\left(\left|\frac{m-\mu}{\sigma}\right|\right)^{1+\frac{1}{1+\left|\frac{1 m-\mu}{\sigma}\right|}}}, \tag{4}
\end{equation*}
$$

where the parameters are determined from MC simulation.
The shape of fake $\chi_{c J}$ candidates, $F_{\mathrm{bkg}}^{\mathrm{non}-\chi_{c J}}$, is described by an ARGUS [19] function.

The fit yields $254 \pm 35\left(K^{*+}, \chi_{c 0}\right)$ events with a statistical significance of $7.2 \sigma, 328 \pm 36\left(K^{*+}, \chi_{c 1}\right)$ events with a statistical significance of $11.6 \sigma$, and $476 \pm 52\left(K^{*+}\right.$, $\chi_{c 2}$ ) events with a statistical significance of $15.2 \sigma$. The statistical significance is determined from the change of the log-likelihood value and the degrees of freedom in the fit when performed with and without a signal component. The 2-D histogram sampled from the composite PDF and the projections of the fit on the $M_{K^{+} \pi^{0}}$ and $M_{\bar{p} K^{*+} \Lambda}$ distributions are shown in Fig. 4.

The BF of $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda$ is calculated by

$$
\begin{align*}
\mathcal{B}= & \frac{N_{\text {sig }}^{\text {obs }}-N_{\mathrm{bkg}}}{\epsilon \cdot N_{\psi(3686)} \cdot \mathcal{B}\left(\psi(3686) \rightarrow \gamma \chi_{c J}\right)} \\
& \times \frac{1}{\mathcal{B}\left(\Lambda \rightarrow p \pi^{-}\right) \cdot \mathcal{B}\left(K^{*+} \rightarrow K^{+} \pi^{0}\right) \cdot \mathcal{B}\left(\pi^{0} \rightarrow \gamma \gamma\right)}, \tag{5}
\end{align*}
$$

where $N_{\text {sig }}^{\text {obs }}$ is the number of signal event returned from the 2-D fit and $N_{\text {bkg }}=11.7 \pm 3.5,5.1 \pm 2.3,4.8 \pm 2.6$ are the numbers of $\left(K^{*}, \chi_{c 0}\right),\left(K^{*}, \chi_{c 1}\right),\left(K^{*}, \chi_{c 2}\right)$ peaking background events, respectively, which is reported in Sec. III B; $N_{\psi(3686)}=(448.1 \pm 2.9) \times 10^{6}$ is the number of $\psi(3686)$ events [5], and $\epsilon$ are detection efficiencies which are determined from MC simulation and found to be $(5.51 \pm 0.05) \%, \quad(7.07 \pm 0.06) \%, \quad$ and $\quad(6.31 \pm 0.06) \%$ for the $\chi_{c 0}, \chi_{c 1}$, and $\chi_{c 2}$ signals, respectively. The BFs $\mathcal{B}\left(\psi(3686) \rightarrow \gamma \chi_{c J}\right), \mathcal{B}\left(\Lambda \rightarrow p \pi^{-}\right), \mathcal{B}\left(K^{*+} \rightarrow K^{+} \pi^{0}\right)$, and $\mathcal{B}\left(\pi^{0} \rightarrow \gamma \gamma\right)$ are taken from Ref. [11]. The BFs of $\chi_{c J} \rightarrow$ $\bar{p} K^{*+} \Lambda$ are measured to be $(4.8 \pm 0.7) \times 10^{-4}$ for the $\chi_{c 0}$ mode, $(5.0 \pm 0.5) \times 10^{-4}$ for the $\chi_{c 1}$ mode, and ( $8.2 \pm$ $0.9) \times 10^{-4}$ for the $\chi_{c 2}$ mode, where the uncertainties are statistical only.

## IV. STUDY OF $\psi(\mathbf{3 6 8 6}) \rightarrow \bar{p} K^{*+} \Lambda$

## A. Event selection

Events are selected containing at least two photons, one $\bar{p}$, one $K^{+}$, and one $\Lambda$ candidate, identified using the same criteria as employed in the $\psi(3686) \rightarrow \gamma \bar{p} K^{*+} \Lambda$ analysis. The selected particles are subjected to a 5C kinematic fit
under the hypothesis of $\psi(3686) \rightarrow \bar{p} K^{+} \pi^{0} \Lambda$, with the invariant mass of the two photons constrained to the $\pi^{0}$ mass. The $\chi^{2}$ of the 5 C fit is required to be less than 100 . For events with more than one combination meeting this requirement, only the combination with the smallest $\chi^{2}$ is retained for further analysis. To veto backgrounds from $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \pi^{0} \Lambda$ and $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \Lambda$, an alternative 5 C (4C) kinematic fit is performed under the $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \pi^{0} \Lambda\left(\gamma \bar{p} K^{+} \Lambda\right)$ hypothesis. We further require that the confidence level of the kinematic fit for the $\psi(3686) \rightarrow \bar{p} K^{+} \pi^{0} \Lambda$ assignment is larger than those of the $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \pi^{0} \Lambda$ and $\psi(3686) \rightarrow \gamma \bar{p} K^{+} \Lambda$ hypotheses.

The distribution of $M_{K^{+} \pi^{0}}$ versus $M_{p \pi^{-}}$is shown in Fig. 5(a), where $K^{*+}$ and $\Lambda$ signals are visible. The $\Lambda$ candidates are selected by requiring $\left|M_{p \pi^{-}}-M_{\Lambda}\right|<$ $6 \mathrm{MeV} / c^{2}$ and $K^{*+}$ candidates are selected by requiring $\left|M_{K^{+} \pi^{0}}-M_{K^{*+}}\right|<0.1 \mathrm{GeV} / c^{2}$. The $K^{*+}$ sidebands are defined to be $1.1<M_{K^{+} \pi^{0}}<1.2 \mathrm{GeV} / c^{2}$ and $0.65<$ $M_{K^{+} \pi^{0}}<0.75 \mathrm{GeV} / c^{2}$. The distribution of $M_{p \pi^{-}}$for events within the $K^{*+}$ signal region is shown in Fig. 5(b). The mass spectra of $\bar{p} K^{*+}, \bar{p} \Lambda, K^{*+} \Lambda$, and Dalitz plot after the application of all selection criteria are shown in Fig. 6. A near-threshold structure in the $M_{\bar{p} \Lambda}$ is fitted with a $1.7 \sigma$ signficance, using the same parametrization as in the $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda$ analysis.

## B. Background study

Using an inclusive MC sample of $506 \times 10^{6} \psi(3686)$ events, the background from fake $\Lambda$ is found together with fake $K^{*+}$. The sources of background can be categorized into two types: peaking background events with genuine $K^{*+}$ mesons in the final state and nonpeaking background events with fake $K^{*+}$ candidates. The nonpeaking background can be estimated from a fit to the $M_{K^{+} \pi^{0}}$ spectrum. The major peaking backgrounds are found to be: $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda(J=0,1,2)$ and $\psi(3686) \rightarrow \bar{p} K^{*+} \Sigma^{0}, \Sigma^{0} \rightarrow \gamma \Lambda$. Corresponding exclusive MC samples are generated for further studies. The selection criteria are applied to these exclusive MC samples and the number of surviving events are normalized by the


FIG. 5. (a) Distribution of $M_{K^{+} \pi^{0}}$ versus $M_{p \pi^{-}}$. The box indicates the signal region. (b) Invariant mass distribution of $p \pi^{-}$. The arrows indicates the mass window used in the selection.


FIG. 6. Invariant mass spectra of (a) $M_{\bar{p} K^{*+}}$, (b) $M_{\bar{p} \Lambda}$, and (c) $M_{K^{*+} \Lambda^{\prime}}$. The dots with error bars are data. The shaded histograms are background from inclusive MC sample. The dashed lines are background that are estimated from the $K^{*+}$ sidebands and are normalized to the signal region. The solid lines are the sum of phase-space MC sample and non- $K^{*+}$ background that are normalized to signal yields. (d) Dalitz plot of $\bar{p} K^{*+} \Lambda$.

BFs of the relevant decay processes. The normalized number of $\psi(3686) \rightarrow \bar{p} K^{*+} \Sigma^{0}$ background events is $5.2 \pm 1.1$ and the expected numbers of $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow$ $\gamma \bar{p} K^{*+} \Lambda(J=0,1,2)$ background decays are $1.9 \pm 0.3$, $4.5 \pm 0.5$ and $8.8 \pm 1.0$, respectively.

A data sample of $2.93 \mathrm{fb}^{-1}$ [14] collected at $\sqrt{s}=$ 3.77 GeV is used to investigate possible background from continuum processes. After normalizing to the integrated luminosity of the $\psi(3686)$ data sample, $164.1 \pm 9.5$ events survive and a clear $K^{*+}$ peak is found in the $K^{+} \pi^{0}$ mass spectrum. This background yield is cross-checked by repeating the procedure on the data sample of $44.5 \mathrm{pb}^{-1}$ [20] collected at $\sqrt{s}=3.65 \mathrm{GeV}$, and a compatible result of $207 \pm 61$ events is obtained, after normalization.


FIG. 7. Invariant-mass spectrum of $K^{+} \pi^{0}$, showing the fit result. The dots with error bars are data and the solid curve shows the fit. The short-dashed curve is $K^{*+}$ signal and the longdashed curve is nonpeaking background.

## C. Branching fraction measurement of $\boldsymbol{\psi}(\mathbf{3 6 8 6}) \rightarrow \bar{p} K^{*+} \Lambda$

An unbinned maximum likelihood fit is performed to the distribution of $M_{K^{+} \pi^{0}}$ (Fig. 7) to extract the number of $K^{*+}$ signal events. The $K^{*+}$ signal shape is described by a $P-$ wave BW function convolved with a double-Gaussian function, and the background shape is described by a truncated polynomial function. The definitions of these functions are the same as those introduced in Sec. III C. The fit result is shown in Fig. 7.

The BF of $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$ is calculated according to

$$
\begin{align*}
\mathcal{B}= & \frac{N_{\mathrm{sig}}^{\mathrm{obs}}-N_{\mathrm{bkg}}}{\epsilon \cdot N_{\psi(3686)} \cdot \mathcal{B}\left(\Lambda \rightarrow p \pi^{-}\right)} \\
& \times \frac{1}{\mathcal{B}\left(K^{*+} \rightarrow K^{+} \pi^{0}\right) \cdot \mathcal{B}\left(\pi^{0} \rightarrow \gamma \gamma\right)}, \tag{6}
\end{align*}
$$

where $N_{\text {sig }}^{\mathrm{obs}}=1011 \pm 60$ is number of $K^{*+}$ signal events obtained from the fit, $N_{\text {bkg }}=20.4 \pm 1.6$ is the number of peaking background events reported in Sec. IV B, and $\epsilon$ is the detection efficiency, $(14.0 \pm 0.1) \%$, estimated from MC simulation. The $\mathcal{B}\left(\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda\right)$ is measured to be $(6.3 \pm 0.5) \times 10^{-5}$, where the uncertainty is statistical only.

## V. SYSTEMATIC UNCERTAINTIES

Systematic uncertainties on the BF measurements arise from a variety of sources:

Tracking efficiency. The uncertainty due to data-MC difference in the tracking efficiency is $1 \%$ for each charged track coming from a primary vertex according to a study of $J / \psi \rightarrow K^{*} \bar{K}$ and $J / \psi \rightarrow p \bar{p} \pi^{+} \pi^{-}$events. For each track from $\Lambda$, the uncertainty is also $1 \%$ from analysis of $J / \psi \rightarrow$ $\bar{p} K^{+} \Lambda$ events [4].

PID efficiency. The candidates require tracks to be identified as $p, \bar{p}, K^{+}$, or $\pi^{-}$. The PID efficiency have been investigated using control samples of $J / \psi \rightarrow$ $K_{S}^{0} K^{ \pm} \pi^{ \pm}$and $J / \psi \rightarrow p \bar{p} \pi^{+} \pi^{-} \quad[21,22]$. The uncertainty is assigned to be $1 \%$ per charged track.

Photon detection efficiency. The photon detection efficiency was studied in the analysis of $J / \psi \rightarrow \rho \pi$ decays [21]. The difference in the detection efficiency between the data and MC simulation is taken as the systematic uncertainty from this source, and $1 \%$ is assigned for each photon.
$\Lambda$ mass window. The systematic uncertainty from the requirement on the $\Lambda$ signal region is estimated by smearing the $p \pi^{-}$invariant mass in the signal MC sample with a Gaussian function to compensate for the resolution difference between data and MC simulation. The smearing parameters are determined by fitting the $\Lambda$ distribution in data with the MC shape convolved with a Gaussian function. The difference in the detection efficiency as determined from signal MC sample with and without the extra smearing is taken as the systematic uncertainty.

Kinematic fit. The systematic uncertainty due to kinematic fitting is estimated by correcting the helix parameters of charged tracks according the method described in Ref. [23]. The differences in the detection efficiency between the MC samples with and without this correction are taken as the uncertainties, which are $0.1 \%, 0.5 \%$, and $0.2 \%$ for $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda(J=0,1,2)$ and $1.4 \%$ for $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$.

Fit range. To estimate the systematic uncertainty due to fit range, several alternative fits in different ranges are performed. The resulting largest difference in the BF is assigned as the systematic uncertainty.

Signal shape. To estimate the uncertainty due to the choice of signal shape, the $K^{*+}$ and $\chi_{c J}$ signal line shapes are replaced by alternative fits using MC shapes and the resulting differences in the BFs are assigned as systematic uncertainties.

Background shape. In the measurements of $\mathcal{B}\left(\chi_{c J} \rightarrow\right.$ $\left.\bar{p} K^{*+} \Lambda\right)$ and $\mathcal{B}\left(\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda\right)$, the $\chi_{c J}$ background shape is described by an ARGUS function and the $K^{*+}$ background shape is described by a second-order truncated polynomial function. To estimate the systematic uncertainty due to choice of background shape, an alternative fit is performed in which the ARGUS function is replaced with a second-order Chebychev polynomial function and the $K^{*+}$ signal is described with a third-order truncated polynomial. The change in the measured BF is assigned as the corresponding systematic uncertainty.

Others. The uncertainty due to the number of $\psi(3686)$ events is $0.7 \%$ [5]. The systematic uncertainties associated

TABLE I. Summary of systematic uncertainties (in \%) in the measured BFs of $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda$ and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$.

|  | $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda$ |  |  |  |
| :--- | ---: | ---: | ---: | :---: |
| Source | $\chi_{c 0}$ | $\chi_{c 1}$ | $\chi_{c 2}$ | $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$ |
| MDC Tracking | 4.0 | 4.0 | 4.0 | 4.0 |
| PID efficiency | 4.0 | 4.0 | 4.0 | 4.0 |
| Photon detection | 3.0 | 3.0 | 3.0 | 2.0 |
| $\Lambda$ mass window | 0.1 | 0.1 | 0.1 | 0.1 |
| Kinematic fit | 0.1 | 0.5 | 0.2 | 1.4 |
| Fit range | 5.9 | 2.1 | 2.0 | 3.0 |
| Signal shape | 4.9 | 3.8 | 4.1 | 3.4 |
| Background shape | 1.3 | 2.0 | 0.7 | 1.1 |
| Number of $\psi(3686)$ events | 0.7 | 0.7 | 0.7 | 0.7 |
| $\mathcal{B}\left(\Lambda \rightarrow p \pi^{-}\right)$ | 0.8 | 0.8 | 0.8 | 0.8 |
| $\mathcal{B}\left(\psi(3686) \rightarrow \gamma \chi_{c J}\right)$ | 2.0 | 2.5 | 2.1 | $\cdots$ |
| Total | 10.3 | 8.5 | 8.2 | 7.8 |

with the intermediate-decay BFs of $\psi(3686) \rightarrow \gamma \chi_{c J}$ and $\Lambda \rightarrow p \pi^{-}$are taken from the PDG [11].

The above systematic uncertainties are summarized in Table I. The total systematic uncertainty is calculated by assuming the individual components to be independent, and adding their magnitude in quadrature.

## VI. RESULTS AND SUMMARY

The processes $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$ are observed for the first time, using $448.1 \times 10^{6} \psi(3686)$ events collected with the BESIII detector. Measurements of the $\mathcal{B}\left(\psi(3686) \rightarrow \gamma \chi_{c J}\right)$. $\mathcal{B}\left(\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda\right)$ and $\mathcal{B}\left(\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda\right)$ are performed, for which the results are listed in Table II. For the processes of $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda(J=0,1,2)$ and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$, no significant substructure is observed in the invariant-mass spectra of $\bar{p} K^{*+}$ and $K^{*+} \Lambda$. The $\bar{p} \Lambda$ mass spectrum is also compatible with the absence of substructure, although fits for possible excesses in the threshold region return results of around two sigma significance in each of the four cases. The new

TABLE II. The BFs of $\psi(3686) \rightarrow \gamma \chi_{c J} \rightarrow \gamma \bar{p} K^{*+} \Lambda$, $\chi_{c J} \rightarrow \bar{p} K^{*+} \Lambda$, and $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$, where the first uncertainties are statistical and the second ones systematic.

| Decay channel | Branching fraction |
| :--- | :---: |
| $\psi(3686) \rightarrow \gamma \chi_{c 0} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ | $(4.7 \pm 0.7 \pm 0.5) \times 10^{-5}$ |
| $\psi(3686) \rightarrow \gamma \chi_{c 1} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ | $(4.8 \pm 0.5 \pm 0.4) \times 10^{-5}$ |
| $\psi(3686) \rightarrow \gamma \chi_{c 2} \rightarrow \gamma \bar{p} K^{*+} \Lambda$ | $(7.8 \pm 0.9 \pm 0.6) \times 10^{-5}$ |
| $\chi_{c 0} \rightarrow \bar{p} K^{*+} \Lambda$ | $(4.8 \pm 0.7 \pm 0.5) \times 10^{-4}$ |
| $\chi_{c 1} \rightarrow \bar{p} K^{*+} \Lambda$ | $(5.0 \pm 0.5 \pm 0.4) \times 10^{-4}$ |
| $\chi_{c 2} \rightarrow \bar{p} K^{*+} \Lambda$ | $(8.2 \pm 0.9 \pm 0.7) \times 10^{-4}$ |
| $\psi(3686) \rightarrow \bar{p} K^{*+} \Lambda$ | $(6.3 \pm 0.5 \pm 0.5) \times 10^{-5}$ |

measurements provide more information for understanding the mechanisms of charmonium decays.

## ACKNOWLEDGMENTS

The BESIII collaboration thanks the staff of BEPCII and the IHEP computing center for their strong support. This work is supported in part by National Key Basic Research Program of China under Contract No. 2015CB856700; National Natural Science Foundation of China (NSFC) under Contracts No. 11335008, No. 11425524, No. 11625523, No. 11635010, No. 11735014; the Chinese Academy of Sciences (CAS) Large-Scale Scientific Facility Program; the CAS Center for Excellence in Particle Physics (CCEPP); Joint Large-Scale Scientific Facility Funds of the NSFC and CAS under Contracts No. U1532257, No. U1532258, No. U1732263; CAS Key Research Program of Frontier Sciences under Contracts

No. QYZDJ-SSW-SLH003, No. QYZDJ-SSW-SLH040; 100 Talents Program of CAS; INPAC and Shanghai Key Laboratory for Particle Physics and Cosmology; German Research Foundation DFG under Contract No. Collaborative Research Center CRC 1044, FOR 2359; Istituto Nazionale di Fisica Nucleare, Italy; Koninklijke Nederlandse Akademie van Wetenschappen (KNAW) under Contract No. 530-4CDP03; Ministry of Development of Turkey under Contract No. DPT2006K120470; National Science and Technology fund; The Knut and Alice Wallenberg Foundation (Sweden) under Contract No. 2016.0157; The Royal Society, UK under Contract No. DH160214; The Swedish Research Council; U.S. Department of Energy under Contracts No. DE-FG02-05ER41374, No. DE-SC-0010118, No. DE-SC0012069; University of Groningen (RuG) and the Helmholtzzentrum fuer Schwerionenforschung GmbH (GSI), Darmstadt.
[1] E. Klempt and J. M. Richard, Rev. Mod. Phys. 82, 1095 (2010).
[2] B. S. Zou, Nucl. Phys. A684, 330 (2001).
[3] M. Ablikim et al. (BES Collaboration), Phys. Rev. Lett. 93, 112002 (2004).
[4] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 87, 012007 (2013).
[5] M. Ablikim et al. (BESIII Collaboration), Chin. Phys. C 42, 023001 (2018).
[6] M. Ablikim et al. (BESIII Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 614, 345 (2010).
[7] S. Agostinelli et al. (GEANT4 Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 506, 250 (2003).
[8] S. Jadach, B. Ward, and Z. Was, Phys. Rev. D 63, 113009 (2001).
[9] D. J. Lange, Nucl. Instrum. Methods Phys. Res., Sect. A 462, 152 (2001).
[10] R. G. Ping, Chin. Phys. C 32, 599 (2008).
[11] M. Tanabashi et al. (Particle Data Group), Phys. Rev. D 98, 030001 (2018).
[12] J. C. Chen, G. S. Huang, X. R. Qi, D. H. Zhang, and Y. S. Zhu, Phys. Rev. D 62, 034003 (2000).
[13] G. Karl, S. Meshkov, and J. L. Rosner, Phys. Rev. D 13, 1203 (1976).
[14] M. Ablikim et al. (BESIII Collaboration), Phys. Lett. B 753, 629 (2016).
[15] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 87, 092006 (2013).
[16] V. M. Malyshev et al., Int. J. Mod. Phys. Conf. Ser. 02, 188 (2011).
[17] S. U. Chung, Phys. Rev. D 57, 431 (1998).
[18] S. Chekanov et al. (ZEUS Collaboration), Eur. Phys. J. C 44, 351 (2005).
[19] H. Albrecht et al. (ARGUS Collaboration), Phys. Lett. B 241, 278 (1990).
[20] M. Ablikim et al. (BESIII Collaboration), Chin. Phys. C 37, 123001 (2013).
[21] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 83, 112005 (2011).
[22] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 85, 092012 (2012).
[23] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 87, 012002 (2013).


[^0]:    * Corresponding author. zhouqiao@ihep.ac.cn
    ${ }^{\text {a }}$ Also at Bogazici University, 34342 Istanbul, Turkey.
    ${ }^{\mathrm{b}}$ Also at the Moscow Institute of Physics and Technology, Moscow 141700, Russia.
    ${ }^{\text {c }}$ Also at the Functional Electronics Laboratory, Tomsk State University, Tomsk, 634050, Russia.
    ${ }^{\text {d }}$ Also at the Novosibirsk State University, Novosibirsk, 630090, Russia.
    ${ }^{\text {e }}$ Also at the NRC "Kurchatov Institute", PNPI, 188300, Gatchina, Russia.
    ${ }^{\text {f }}$ Also at Istanbul Arel University, 34295 Istanbul, Turkey.
    ${ }^{\mathrm{g}}$ Also at Goethe University Frankfurt, 60323 Frankfurt am Main, Germany.
    ${ }^{h}$ Also at Key Laboratory for Particle Physics, Astrophysics and Cosmology, Ministry of Education; Shanghai Key Laboratory for Particle Physics and Cosmology; Institute of Nuclear and Particle Physics, Shanghai 200240, People's Republic of China.
    ${ }^{i}$ Also at Government College Women University, Sialkot 51310. Punjab, Pakistan.
    ${ }^{\mathrm{j}}$ Also at Key Laboratory of Nuclear Physics and Ion-beam Application (MOE) and Institute of Modern Physics, Fudan University, Shanghai 200443, People's Republic of China.
    ${ }^{k}$ Also at Harvard University, Department of Physics, Cambridge, Massachusetts 02138, USA.

    Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP ${ }^{3}$.

